## UNIVERSITY OF CALIFORNIA

Santa Barbara

Area-efficient Neuromorphic Silicon Circuits and Architectures using Spatial and Spatio-

**Temporal Approaches** 

A dissertation submitted in partial satisfaction of the requirements for the degree Doctor of Philosophy in Electrical and Computer Engineering

by

Melika Payvand

Committee in charge:

Professor Luke Theogarajan, Chair

Professor Forrest Brewer

Professor Dmitri Strukov

Professor K.-T. Tim Cheng

Professor Wei Lu

December 2016

The dissertation of Melika Payvand is approved.

Forrest Brewer

Dmitri Strukov

K. -T. Tim Cheng

Wei Lu

Luke Theogarajan, Committee Chair

December 2016

Area-efficient Neuromorphic Silicon Circuits and Architectures using Spatial and Spatio-

Temporal Approaches

Copyright © 2016

by

Melika Payvand

#### ACKNOWLEDGEMENTS

The past 6 years in UCSB has truly been a life journey in many different aspects. It was a process of scientific, philosophical, intellectual, psychological and social growth for me. When I think back I cannot believe how far I've come as a person and I owe this to the fantastic people I've met here, in Santa Barbara. I want to dedicate my thesis to them as they formed these unforgettable years for me.

My advisor, professor Luke Theogarajan, who was always a source of inspiration and a true mentor, in science and in life. He truly cared about the well-being of all of his students and I'm honored to have been one of them.

Professor Forrest Brewer who always encouraged curiosity and his breadth of knowledge was inspirational. He always made me feel that there is so much to learn.

Professor Dmitri Strukov, Professor Tim Cheng and Professor Wei Lu who provided other perspectives in MURI project and they were always happy to help and listen to me.

Bruno Silva, whose perspective in life changed me to my core. His peace calmed me down, made me believe that any achievement in life requires patience and good things happen to people who wait. He brought a sense of meaning and gratitude to my life which nobody has ever had.

Advait Madhavan, who always offered a hand when I was falling. Who believed in me when I didn't and who listened to me when no-one else did. Can't thank him enough. Doing tape-out with him is my favorite part of grad school ©

Amirali Ghofrani, who was family. His support, warmth and positivity always fueled me. He never failed to bring happiness.

iv

Doing a tape out with Amirali, Advait and Miguel Lastras was an incredible experience. We worked together as a team and learned so much from each other. I very much appreciate Miguel's drive in that project for if it wasn't for his belief in memristors, that chip would have never got to where it did.

Danielle Morton, who patiently taught me all she thought I should know when I joined the group and was always happy to help. Her perseverance was always a source of admiration for me.

Anahita Mirtabatabayi for when she is around everything is better. She shaped the structure of my life in Santa Barbara and was always a role model for me as a strong woman.

Tanya Das and Oana Catu who never failed to bring joy to my life. They were there when I needed them the most and gave me so much love.

All of my current and past colleagues in Biomimmetic Circuits and Nano Systems group for providing such a friendly environment to discuss circuits, science and life and to share laughter and joy. I appreciate each and every one of them.

Colleen and Alf, who were my family. Can't thank them enough. They care for me as their daughter and never failed to give their support.

And, to my family. For they gave me all they had not for the past 6 years but since I started existing.

My parents who ignited the flames of desire for achievement and success in me.

My sister whose unconditional love warms my heart.

My grandma who is happy with my happiness and sad with my sadness.

My aunt and uncle who embraced me with all they had when I moved to the US.

THANK YOU all for being part of my life and forming my great years of graduate school. I couldn't have asked for more.

"The science of the mind can only have for its proper goal the understanding of human nature by every human being, and through its use, brings peace to every human soul."

—Alfred Adler

### VITA OF MELIKA PAYVAND

## December 2016

## **EDUCATION**

PhD, University of California Santa Barbara, Electrical and Computer Engineering Advisor: Prof. Luke Theogarajan, December 2016

M.S. University of California Santa Barbara, Electrical and Computer Engineering, Septermber 2012

B.S. University of Tehran, Iran. Electrical and Computer Engineering, July 2010

## SUMMARY OF SKILLS

o IC Design, Layout and Test: Full design flow of chip design from transistor level to layout to post-layout simulations and testing: Neuromorphic VLSI, Analog/ Digital/ Mixed Signal Circuit Design, FPGA Design, PCB Design

Machine Learning: Logistic/Softmax Regression, Supervised/Unsupervised Learning,
 Convolutional Neural Networks, Auto-encoders, PCA, Sparse Coding, etc.

o Computational Neuroscience: Spike Encoding/Decoding, Information Theory

o Resistive Switching and Memristive Device and Application

### RESEARCH AND WORK EXPERIENCE

o Developed A Novel Spatio-Temporal Coding Algorithms for Neuromorphic Chip Applications: This algorithm uses a combinatorial scheme in spiking patterns of neurons which learn to recognize patterns in a completely unsupervised fashion. This results in significantly reducing the number of connections required to do similar tasks using other counterpart algorithms, Summer 2015-Present

o Tape-out: Configurable CMOS Spiking Neurons for 3D-Memristive Synapses Design, layout and tape-out of a neuromorphic chip containing an array of CMOS spiking neurons. Spike shapes are engineered to enable STDP for memristive crossbars and are fully configurable. The circuit is designed fully asynchronously to enable online unsupervised learning. The chip is designed in Silterra 180nm. Winer 2015

o Developed a Mapping from Connectivity Domain Available in CMOL Architecture to Localized Neural Receptive Fields: Explored the use of large fan-in locally connected spiking silicon neurons readily available in CMOL architecture to solve edge recognition in images via unsupervised learning. Spring 2015

o Tape-out: Configurable CMOS Memory Platform for 3D Memristor Integration Involved in a collaborative CMOL (CMOS-Molecular devices) memory development project. Design, layout and test of the first CMOS memory controller platform for the memristive memory array in a hybrid/3D architecture. Testing resulted in full functionality of the chip which was fabricated in On-Semi 3M2P 0.5um occupying 2X2mm2. Summer 2014-Winter 2014

o Tape-out: Floating Gate Transistor and Photodiode Characterization

ix

Design, layout and tape-out of a chip to characterize floating gate transistor current as a result of hot electron injection into the floating gate. A current sensing scheme using a WTA circuit was utilized to detect the change in current. Photo-diode current sensing circuit was designed using a current to frequency conversion for a digital read out. Winter-Spring 2013

## PUBLICATIONS

M. Payvand, L. Theogarjan "Winners-Share- All: Towards Exploiting the Information Capacity in Temporal Codes", In Manuscript 2016

M. Payvand, L. Theogarajan, "Exploiting Local Connectivity of CMOL Architecture for Highly Parallel Orientation Selective Neuromorphic Chips", IEEE/ACM International Symposium on Nanoscale Architectures (NANOARCH), Boston, Massachusetts, USA, July 2015

M. Payvand, A. Madhavan, M. Lastras, A. Ghofrani, J. Rofeh, T. Cheng, D. Strukov, L. Theogarajan, "A configurable CMOS memory platform for 3D integrated memristors", ISCAS 2015

M. Payvand, J. Rofeh, A. Sodhi, L. Theogarajan, "A CMOS-memristive self -learning neural network for pattern classification applications", Nanoarch, July 2014, Paris, France
J. Rofeh, A. Sodhi, M. Payvand, M. Lastras, A. Ghofrani, et al, "Vertical integration of memristors onto foundry CMOS dies using wafer-scale integration", ECTC 2015, IEEE 65th.
A. Ghofrani, M. Lastras, S. Gabba, M. Payvand, W. Lu, L. Theograjan, T. Cheng, "A low-power variation-aware adaptive write scheme for access-transistor-free memristive memory", JETC, 2015

# AWARDS

Awarded University of California Doctoral Student Travel Grant, July 2015

Awarded Graduate Student Researcher Fellowship (GSR), UC Santa Barbara, 2012-Present

Awarded Best Teaching Assistant Award, Spring 2011

Picked Among the 5% Exceptional Students, Department of ECE, University of Tehran,

2008-2010

Ranked 164 among 500,000 participants nationwide in "University Entrance Exam", Iran, Summer 2005

## ABSTRACT

# Area-efficient Neuromorphic Silicon Architectures using Spatial and Spatio-Temporal

Approaches

by

## Melika Payvand

In the field of neuromorphic VLSI connectivity is a huge bottleneck in implementing braininspired circuits due to the large number of synapses needed for performing brain-like functions. (E.g. pattern recognition, classification, etc.). In this thesis I have addressed this problem using a two pronged approach namely *spatial* and *temporal*.

**Spatial**: The real-estate occupied by silicon synapses have been an impediment to implementing neuromorphic circuits. In recent years, memristors have emerged as a nano-scale analog synapse. Furthermore, these nano-devices can be integrated on top of CMOS chips enabling the realization of dense neural networks. As a first step in realizing this vision, a programmable CMOS chip enabling direct integration of memristors was realized. In a collaborative MURI project, a CMOS memory platform was designed for the memristive memory array in a hybrid/3D architecture (CMOL architecture) and memristors were successfully integrated on top of it. After demonstrating feasibility of post-CMOS integration of memristors, a second design containing an array of spiking CMOS neurons was designed in a 5mm x 5mm chip in a 180nm CMOS process to explore the role of memristors as synapses in neuromorphic chips.

**Temporal**: While physical miniaturization by integrating memristors is one facet of realizing area-efficient neural networks, on-chip routing between silicon neurons prevents the complete realization of complex networks containing large number of neurons. A promising solution for the connectivity problem is to employ spatio-temporal coding to encode neuronal information in the time of arrival of the spikes. Temporal codes open up a whole new range of coding schemes which not only are energy efficient (computation with one spike) but also have much larger information capacity than their conventional counterparts. This can result in reducing the number of connections to do similar tasks with traditional rate-based methods.

By choosing an efficient temporal coding scheme we developed a system architecture by which pattern classification can be done using a "Winners-share-all" instead of a "Winner-takes-all" mechanism. Winner-takes-all limits the code space to the number of output neurons, meaning n output neurons can only classify n pattern. In winners-share-all we exploit the code space provided by the temporal code by training different combination of k out of n neurons to fire together in response to different patterns. Optimal values of k in order to maximize information capacity using n output neurons were theoretically determined and utilized. An unsupervised network of 3 layers was trained to classify 14 patterns of 15 x 15 pixels while using only 6 output neurons to demonstrate the power of the technique. The reduction in the number of output neurons results in the reduction of number of training parameters and results in lower power, area and memory required for the same functionality.

# Table of Contents

| I. Chapter 1: Introduction   | 1      |
|--|--------|
| 1.1 Silicon Neurons  | 3      |
| 1.2 Silicon synapses   | 4      |
| 1.2.1 Capacitors   | 4      |
| 1.2.2 Flash  | 6      |
| 1.2.3 Multiple SRAMs   | 7      |
| 1.3 Overview   | 8      |
| 1.3.1 Spatial approach: Memristors   | 8      |
| 1.3.2 Spatio-temporal Coding Approach  | 9      |
| II. Chapter 2: Memristors and Memristive Architectures   | 10     |
| 2.1 What is a memristor?   | 11     |
| 2.2 Memristors as Memory Elements  | 14     |
| 2.2.1 Crossbar   | 16     |
| 2.2.2 CMOL Architecture  |        |
| III. Chapter 3: Memory Access controller for Memristor Applications (  | (MAMA) |
|  | 22     |
| Cnip   |        |
| 3.1 Chip Architecture  |        |
| <ul><li>3.1 Chip Architecture</li></ul>  |        |
| <ul> <li>3.1 Chip Architecture</li></ul>   |        |
| <ul> <li>3.1 Chip Architecture</li></ul>   |        |
| <ul> <li>3.1 Chip Architecture</li></ul>   |        |
| <ul> <li>Chip</li> <li>3.1 Chip Architecture</li> <li>3.2 Writing Circuitry (CMOS Cell Design)</li> <li>3.3 Sensing Circuitry</li> <li>3.4 Measurement Results</li> <li>3.4.1 Writing Circuitry Characterization</li> <li>3.4.2 Sensing Circuitry Characterization</li> </ul>                                      |        |
| <ul> <li>3.1 Chip Architecture</li> <li>3.2 Writing Circuitry (CMOS Cell Design)</li> <li>3.3 Sensing Circuitry</li> <li>3.4 Measurement Results.</li> <li>3.4.1 Writing Circuitry Characterization</li> <li>3.4.2 Sensing Circuitry Characterization</li> <li>3.4.3 Memristor Characterization Results</li> </ul> |        |
| <ul> <li>3.1 Chip Architecture</li></ul>   |        |
| <ul> <li>Chip.</li> <li>3.1 Chip Architecture</li></ul>  |        |
| <ul> <li>Chip</li></ul>  |        |

| 5.2 Temporal Codes  |
|---|
| 5.3 Time as Basis for Information Encoding                              |
| 5.4 Rank Order Code   |
| 5.5 Winners-Share-All (WSA)   |
| VI. Chapter 6: Applying WSA to a Classification Problem                 |
| 6.1 Network Architecture  |
| 6.1.1 Neuron's Model  |
| 6.1.2 Synapse Model   |
| 6.2 Layer 1: Converting Pixel Intensity into Spikes                     |
| 6.3 Layer 2: Extracting features from the Images                        |
| 6.4 Layer 3: Classification   |
| 6.4.1 Challenge 1: Learning71   |
| 6.4.2 Challenge 2: Inhibition   |
| 6.4.3 Challenge 3: Correlation in the input patterns                    |
| 6.4.4 Challenge 4: Greedy Attractor77                                   |
| 6.5 Results   |
| 6.5.1 Weight Evolution  |
| 6.5.2 Output Neurons Output   |
| 6.5.3 Classification  |
| VII. Conclusion and Future Work   |
| 7.1 Conclusion  |
| 7.2 Future Directions   |
| References  |
| Appendix I: MATLAB Code developed for Layer 1: Image Intensity to Spike |
| Conversion  |
| Appendix II: MATLAB Code developed for Layer 2: Extracting Features98   |
| Appendix III: MATLAB Code Developed for Layer 3: Classification101      |

# List of Figures

| Figure I-1 Axon Hillock Neuron Model [34]   |
|---|
| Figure I-2 The bistability circuit will drive the w node towards one of its two stable            |
| states.Figure adopted from [3]5   |
| Figure I-3 P-type Synapse Transistor [35]6  |
| Figure II-1Memristor realization and typical hysteretic I-V behavior. (a) OFF state: An           |
| initial fil- ament is formed during a one-time formation process. No conductive channel           |
| exists; thus the device is in high resistance state. (b) Set process: positive voltage drifts the |
| dopants toward the filament, forming a channel, and decreasing the resistance. (c) ON state: a    |
| low-resistance channel is formed between the two electrodes. (d) Reset process: Applying a        |
| negative voltage repels the dopants and ruptures the channel, increasing the resistance.          |
| Adopted from [10]   |
| Figure II-2 Memristors' main operating regions; Green: Diode region where tiny current            |
| passes through the device under the application of electric field. Yellow: Red region where       |
| enough current passes through the memristors to sense the state of the device without             |
| changing its state. Red: Switching region where the memristor switches from one state to          |
| another   |
| Figure II-3 Standard memory architecture14  |
| Figure II-4 1T-1R architecture. Memristors are accessed through selecting the series              |
| transistor15  |
| Figure II-5 Crossbar memristor array with selected bits for reading and writing [11]16            |
| Figure II-6 CMOS Level Chip Architecture [11]17   |
| Figure II-7 Cutting large crossbars into many small ones. Decoding the crossbar is                |
| equivalent to decoding a "blue pin" and decoding a memristor within that mini crossbar is         |

Figure III-4 a) Chip micrograph. Different parts of the chip are shown. b) Individual

devices integrated on the chip......27

Figure III-6 a) Write circuitry characterization. As the resistive load decreases, the writing voltage drop across the load also decreases. b) Read circuitry characterization. The

Figure III-7 3D-integrated memristors on top of MAMA chip. on the left,

Figure IV-4 Membrane voltage waveforms. Pre-and post-synaptic membrane voltages for the situations of positive  $\Delta T$  (A) and negative  $\Delta T$  (B). Figure is taken from [18]......35

Figure IV-7 Complete neuron's model with feedforward and feedback pulse shapers. ....38

| Figure IV-8 Leaky integrate and fire neuron (1)   |
|---|
| Figure IV-9 Leaky integrate and fire neuron (2)40   |
| Figure IV-10 Complete leaky integrate and fire model41                                      |
| Figure IV-11 OpAmp topology employed for the integrator in the LIF neuron. The              |
| OpAmp has an extended common mode range at the input with a class A-B push pull at the      |
| output to drive the memristive crossbar array42   |
| Figure IV-12 Amplifier stay stable for more than 2 orders of magnitude to support the       |
| current needed to program the memristors in the crossbar array43                            |
| Figure IV-13 Desired pulse shape with configurable parameters44                             |
| Figure IV-14 pulse shaper design. Configurability is enabled through the use of DACs        |
| and clks  |
| Figure IV-15 Spectre simulation results illustrating the configurability of the pulse shape |
| through DAC (left) and clk (right)46  |
| Figure IV-16 Complete layout of the LIF neuron with feedforward and feedback pulse          |
| shapers. Red and Blue pins are placed to enable CMOL implementation of memristors for 3D    |
| integration47   |
| Figure IV-17 Inhibition block schematic (left). Layout of one of the 5 sections (right)48   |
| Figure IV-18 Complete layout of the LIF neurons 5x5 array. Each neuron takes an area of     |
| 500 x 500 μm <sup>2</sup>   |
| Figure IV-19 Chip Micrograph in Silterra 180 nm49   |
| Figure V-1 Simple model of the biological neurons (left). First mathematical model of the   |
| neurons (right). Figure is taken from [26]  |

| Figure V-2 Neural pathway from the retina to the inferotemporal cortex, where visual            |
|---|
| objects are recognized. Figure taken from [36]  |
| Figure V-3 Intensity to latency conversion. The stronger the input, the faster the neuron       |
| spikes. Figure is taken from [30]52   |
| Figure V-4 Illustration of using temporal codes for computation. Time is divided into           |
| time windows and information can be encoded depending on which neurons spike in each            |
| time window. Figure is taken from [26]53  |
| Figure V-5 Possible neural codes provided by the temporal coding. Figure is taken from          |
| [37]  |
| Figure V-6 Competitive Learning- Each output neuron represents a cluster. N_A and               |
| N_B represent cluster A and B respectively and $W_A$ and $W_B$ are the centers of the clusters. |
| Upon the arrival of every input pattern, the winner neuron's weights adjust themselves to get   |
| closer to the input pattern   |
| Figure V-7 Emergence of selective responses of each neuron to a specific pattern. Lateral       |
| inhibition is applied as a winner takes all mechanism and competitive learning results in the   |
| assignment of each pattern to the emission of one spike from one neuron. Figure is taken        |
| from [30]   |
| Figure V-8 Comparison of the number of output neurons required to recognize patterns            |
| between WTA (blue) and WSA (red) mechanism. As the number of patterns increase, the             |
| efficiency of using WSA becomes more apparent60   |
| Figure V-9 The case with two similar rank codes in which only the rank of two last              |
| spikes are different61  |
| Figure VI-1 Training set and Test set patterns used for the classification problem63            |

Figure VI-7 Spiking learning algorithm developed for WSA. Calcium concentration models are used as part of the Anti-STDP rule to calculate dwp and dwn......73

Figure VI-9 Habituation neuron designed to ignore the similarities between the input patterns and look for the differences between patterns which helps to separate patterns.......76

| Figure VI-10 Concept of homeostatic plasticity in the brain. Feedback mechanisms are           |
|--|
| applied in order to keep the firing rate of a neuron in a target range. Figures are taken from |
| [32]   |
| Figure VI-11 Neural State Machine (NSM) designed to control the appearance frequency           |
| of the WSA codes   |
| Figure VI-12 Weight evolution showing the weights converging to analog values83                |
| Figure VI-13 Network performance on the test set. On the left, the network accuracy            |
| converges to 87%. On the right, each pattern gets assigned to a unique combination from a      |
| set of 41 codes in the code space  |
| Figure VI-14 Edit distance vs Pattern similarity for all the patterns                          |
| Figure VII-1 400 features extracted from MNIST training set by training an                     |
| autoencoder  |

# I. Chapter 1: Introduction

There has been a long standing dream to make computers that work like the brain and scientist have been working on this problem for decades now. However, the gap between the state-of-the-art computers and the brain is still very large. The most important reasons why are because:

1) Computers and the brain have a fundamentally different way of computing. Computers have a deterministic approach in processing the input data. There are well-defined logic gates which take 0 and 1 logic levels as inputs, and output appropriate 0s and 1s depending on the logic function. Whereas the brain takes a self-organizing method of computation, meaning that it *learns* from mistakes. Let me give the example of throwing a ball into the basket. If we were to *program* a conventional computer to achieve this, all the physical laws of gravity would have had to be defined in the program, taking into account details such as the size of the ball, and also environmental factors such as the wind or rain and ask the computer to *calculate* the initial velocity and direction of throwing the ball in order to make it to the basket. The brain, however, has a completely different approach. The ball is thrown and if it does not make it to the basket, it *learns* from its mistake. The solution to the problem of targeting the ball into the basket overshoots and undershoots until the goal is reached. That's how the brain *self-organizes* the solution to an unknown problem, by trial and error.

2) In computers the execution of instructions is *rather* sequential. The reason why I say "rather" is because today's computers take advantage of a lot of parallelization using GPUs. However, the parallelization works as dividing tasks between different processing cores but execution of each task at a specific core is still sequential. This is while the brain

processes information massively in parallel: millions of processing units all working *at the same time*.

3) While brain uses these millions of processing units in parallel, which are connected to each other through billions of connections, it only consumes a few tens of watts. If we were to run "human-scale" simulations of the brain running in real time, using the best supercomputers, that would consume about 12 Giga watts of power. [1]

The reasons mentioned above makes it clear why building a "brain-inspired" computer is the next computing paradigm. These computers will be

- a) Efficient in terms of energy and space
- b) Scalable to large networks
- c) Flexible enough to run complex behavioral model

Considering how far we have come in silicon industry and all the advances in the field of neuroscience and AI, could make us wonder what is stopping us from making these computers? The answer lies of course in limitations we face because of the physical properties of silicon chips. Below I will talk about the major bottlenecks of building such computers.

#### **Bottlenecks of implementing brain-inspired computers**

Centralized von Neumann architecture is fundamentally not suitable for representing massively interconnected neural networks. In this type of architecture, used in conventional computers, the processing unit and the memory are separated from each other. When there is an instruction to be executed, special part of the memory is addressed, the data is fetched and is processed in the CPU. This is fundamentally in contradiction with how the brain performs the computation where the memory is localized to the processing unit and is distributed all across the brain. In order to make brain-like computers we should also use these distributed computing-memory agents, namely **neurons** and **synapses.** 



Figure I-1 Axon Hillock Neuron Model [34].

# 1.1 Silicon Neurons

Silicon neurons emulate the electro-physiological behavior of real neurons. This may be done at many different levels, from simple models (like leaky integrate-and-fire neurons) to models emulating multiple ion channels and detailed morphology. Depending on the application and the level of sophistication required, different models could be used. Leaky integrate and fire models are less realistic and do not take into account many of the details of what's going on inside a neuronal cell. But they are simple and need very small area since the number of transistors used in the circuit is minimal.

The first leaky integrate and fire model which was proposed by Carver Mead in the late 1980s is shown in Figure I-1. In this circuit, a capacitor that represents the neuron's membrane lipid bilayer integrates input current into the neuron. As soon as the capacitor reaches the neuron's threshold, a pulse  $V_{out}$  is generated, the membrane potential  $V_{mem}$  is reset through the NMOS transistors and the neuron will be ready for the next current injection.

# 1.2 Silicon synapses

Conceptually, synapses can be modeled as the connection between neurons with an associated strength (weight). In fact, synapses are the adaptive learning agents in the brain: Neurons receive inputs and fire, so they have a very specific task: when the membrane potential is above a threshold, they fire. However, the synapse's strength has dynamics and will change in the process of learning. These changes are continuous and *analog* rather than digital. Therefore, in order to mimic the synaptic behavior into the silicon we need nonvolatile *analog* memory storage with locally computed memory updates. Note that in order to perform brain-like functions, a large number of artificial synapses are needed.

Throughout the history of neuromorphic engineering, circuit designers tried many different options as analog memory for artificial synapses. I'll briefly go over each of them below.

## 1.2.1 Capacitors

Capacitors are the first obvious choice for analog memory. They accumulate the charge and develop a voltage across their capacitive plate. The only important problem is that they leak. So they are not truly non-volatile as they slowly lose the charge. However, different solutions have been proposed to overcome this problem. For example, using techniques such as generating negative gate-source voltage across the series transistor in order to reduce the leakage below the "off subthreshold current" [2], or using them only as an analog memory while learning ,and then register the value as a single digital bit depending on the analog value of the capacitor voltage. This is called Fusi learning [3]. The idea is presented in Figure I-2 shown below.



Figure I-2 The bistability circuit will drive the w node towards one of its two stable states. Figure adopted from [3].

In other words, the synapse value is analog in the short term and digital in the long run. The positive feedback loop in the circuit will drive the capacitive charge towards a digital 1 or zero depending on the current value of the capacitor voltage. If the capacitor voltage is higher than a positive V<sub>th,p</sub> it will slowly charge the capacitor through a small subthreshold current to VDD and if that's lower than a negative V<sub>th,n</sub> it will discharge it towards VSS. Although this is a prominent solution, there are two issues rising from it: i) Although some neuromorphic engineers argue that for neural network applications, a few number of bits are enough [4], employing a true analog memory has advantages which I will talk about some of them later in the thesis. Simply put, since digital synapses are a big approximation we could easily end up with relatively large errors on applications such as pattern recognition. ii) One limitation of using one capacitor for each synapse is that it takes a large area on chip. If the technology process does not provide MIM (Metal-Insulator-Metal) capacitor structures, then having a capacitive memory means we need to have a memory array at one part of the chip and having neurons in another part which is employing the von Neumann architecture. For reasons we discussed before using this architecture is fundamentally different from what the brain does



Figure I-3 P-type Synapse Transistor [35].

and will limit us in parallelizing the structure. Even if the technology process provides a MIM capacitor structure, the supporting circuity needed for each synapse in order to enable online-learning is very area-hungry and will only work for small networks.

## 1.2.2 Flash

In the late 90s, C. Diorio and his colleagues in Carver Mead's lab fabricated synapse transistors that not only possessed nonvolatile analog storage, and compute locally their own memory updates, but also allowed local computation of the product of their stored memory value and the applied input. To ensure nonvolatile storage, they used standard floating-gate MOS technology, but adapted the physical processes that write the memory to perform a local learning function [5]. Figure I-3 shows the p-type of this synapse transistor.

The underlying process of non-volatility of the memory lies in trapping electrons in the floating gate by employing hot-electron injection which is a well-known process in MOSFETs.

It occurs in short-channel devices with continuous channel currents, when a high gate voltage is combined with a large potential drop across the short channel. Injecting electrons into the floating gate will cause a negative voltage to develop on the gate and hence it will decrease the threshold voltage of the PMOS, increasing the "weight" of the synapse transistor. On the contrary, in order to remove charge from the floating gate and decrease the synaptic "weight", positive high voltages should be applied to the tunneling implant to remove electrons from the floating gate, thereby increasing the floating gate voltage.

The advantage of this method is that the weight multiplication by the input is done locally and without any extra circuity. So it's area-efficient and local. The disadvantages of using these synapse transistors are i) There is not a full-blown model of these transistors available in CAD tools such as Cadence virtuoso. Therefore, when laying out these devices, the standard CMOS process transistors cannot be used and hence the functionality of these devices cannot be ensured before their fabrication. ii) Increasing and decreasing the weights are not trivial. High voltages are needed in order to facilitate hot-electron-injection and tunneling mechanisms. These high voltages need to be generated on chip (or by connecting from an I/O whose ESD protection diodes have been removed) and will decrease the oxide life time.

## 1.2.3 Multiple SRAMs

Yet another method of building electronic synapses employed by researcher throughout the years have been to use multiple SRAMS [6]. In this method, few bits of memory are devoted to each synapse. Analog values of synapse are digitized using a DAC and are kept in the SRAM. When reading, the SRAM memory bits are fed into an ADC and the analog value is used in the circuit. The advantage of this method is that it's very robust since the memory is kept digitally. The disadvantages are i) it's volatile. So with the loss of power the memory will

be reset. ii) It's very computationally expensive and area inefficient to use an ADC and a DAC for *every* synapse. These ADCs and DACs can be shared but that serializes the process and also needs extra circuitry in order to priority encode which synapse will take use of the shared DAC and the ADC.

# 1.3 Overview

As stated above, one of the most important bottlenecks of building computers that work like the brain, is to make artificial synapses. Although there have been many attempted solutions for this problem, packing a large number of silicon synapses in a small area enabling the local learning remains an issue. In this thesis, I have investigated a two pronged approach namely *spatial* and *temporal* to tackle this problem.

## 1.3.1 Spatial approach: Memristors

In recent years, memristors have emerged as a solution for the connectivity problem. These nano-devices can be densely integrated on top of CMOS chips and can serve as analog memory needed to imitate synapses. What makes memristors a perfect candidate as an artificial synapse is not only because they have a nano-size footprint and they take no silicon space, but also they are non-volatile analog memory. Also, they imitate biological synapses very well since the multiplication of the weight (Memristor's conductance G) to the input current (I) occurs automatically through Ohm's law (I=GV). The adaptive conductance of the material could serve as "analog weights" which develop voltages across the devices, depending on the current passing through them as inputs to the network.

As a first step in realizing integrated memristors as artificial synapses, we designed a programmable CMOS chip enabling direct integration of memristor. In a collaborative MURI

project, a CMOS memory platform was realized for the memristive memory array in a hybrid/3D architecture (CMOL architecture [7]) and memristors were successfully integrated on top of it. After demonstrating feasibility of post-CMOS integration of memristors, we designed a second chip containing an array of spiking CMOS neurons with an area of 5mm x 5mm in a 180nm CMOS process to explore the role of memristors as synapses in neuromorphic chips.

## 1.3.2 Spatio-temporal Coding Approach

While physical miniaturization by integrating memristors is one facet of realizing areaefficient neural networks, on-chip routing between silicon neurons prevents the complete realization of complex networks containing large number of neurons. A promising solution for the connectivity problem is to employ spatio-temporal coding to encode neuronal information in the time of arrival of the spikes. Temporal codes open up a whole new range of coding schemes which not only are energy efficient (computation with one spike) but also have much larger information capacity than their conventional counterparts. This can result in reducing the number of connections to do similar tasks with traditional rate-based methods.

By choosing an efficient temporal coding scheme, I have developed a system architecture by which pattern classification can be done using a new algorithm dubbed "Winners-share-all" instead of a "Winner-takes-all" mechanism. Winner-takes-all limits the code space to the number of output neurons, meaning n output neurons can only classify n pattern. In winnersshare-all we exploit the code space provided by the temporal code by training different combination of k out of n neurons to fire together in response to different patterns This thesis will be divided into two major parts: Spatial and Spatio-Temporal approach. In Chapter 2,3, and 4, I cover the spatial approach which studies the role of memristors as synapses in neuromorphic chips. In chapter 2, I briefly introduce memristors and talk about some of the background work on different memristive architectures. Chapter 3 will cover the details of the first chip we taped out which incorporated a means for 3D-integrating Memristive Arrays for Memory Applications (MAMA). After demonstrating the feasibility of post-CMOS integration of memristors on MAMA chip, I then explain, in chapter 4, how we took the next step to design an array of spiking CMOS neurons on a second chip to explore the role of memristors as synapses in neuromorphic chips.

The second part of this thesis is devoted to the Spatio-temporal coding approach to reduce the number of connectivity needed on chip by exploring the code space provided by the temporal codes. Chapter 5 will introduce the concept of information encoding in time and a summary of background work on this area. I will then propose the Winners-Share-All (WSA) algorithm using the temporal code and compare it to the conventional Winner-Takes-All (WTA) counterpart. In chapter 6, I describe how I used this new algorithm to perform a rather simple recognition task to cluster 14 letters of English alphabet. And finally chapter 7 will summarize the work of this PhD thesis and discuss the future directions.

# II. Chapter 2: Memristors and Memristive Architectures

As the basic building block of electronics, field effect transistor (FET), approaches the 10nanometer regime, a number of fundamental and practical issues start to emerge due to difficulties in nanometer-resolution fabrication, electrostatic control and power management. New devices and architectures are expected to continue the scaling trend the semiconductor industry has enjoyed in the past decades. Two-terminal resistive switches (also called memristive devices or memristors) have attracted increasing interest as a suitable alternative to complement transistors. [8]. In this chapter I introduce memristors and explain its underlying mechanism. I will also talk about the architectures developed for these nano-devices and how they can be used for neuromorphic applications.

# 2.1 What is a memristor?

As can be guessed by the name, it's a memory resistor: A two-terminal switch which can retain its resistive state based on the history of the applied field and hence it's an analog nonvolatile memory. They are simple passive circuit elements, but their function cannot be replicated by any combination of fundamental resistors, capacitors and inductors [9].

Memristors are typically based on a Metal-Insulator-Metal (MIM) structure. An otherwise insulating film is sandwiched between two conductive electrodes. The choice of material for this MIM structure has been under extensive research with different stacks. The underlying switching mechanism seems to differ for a variety of electrode and memristive materials:

The mechanism can be attributed to a) phase change due to Joule heating in chalcogenidebased phase-change memories. b) conductive filament formation due to Joule heating observed in certain oxides such as TiO2. c) conductive filament formation due to electrochemical redox



Figure II-1Memristor realization and typical hysteretic I-V behavior. (a) OFF state: An initial fil- ament is formed during a one-time formation process. No conductive channel exists; thus the device is in high resistance state. (b) Set process: positive voltage drifts the dopants toward the filament, forming a channel, and decreasing the resistance. (c) ON state: a low-resistance channel is formed between the two electrodes. (d) Reset process: Applying a negative voltage repels the dopants and ruptures the channel, increasing the resistance. Adopted from [10].

processes observed in binary oxides (e.g. NiO, CuO<sub>2</sub>, TiO<sub>2</sub>) or chalcogenides, and polymers d) field-assisted drift/diffusion of ions in amorphous films and e) possible conformational changes in molecules. [8]

Figure II-1 shows an example of a memristors in which Pt is used as the electrode and  $TiO_2$  as the switching material. There are also some oxygen vacancies in the form of  $TiO_{2-x}$  which act as charged dopants and can respond to the electric field. In the initial state, a filament of conductive  $TiO_{2-x}$  is formed in the non-conductive  $TiO_2$  film in an irreversible forming step. However, the formed filament does not connect the two electrodes together and thus the device is in a High Resistance State (HRS). In order to switch the device ON, a sufficiently high positive voltage is applied across the device which attracts positively charged vacancies in the



Figure II-2 Memristors' main operating regions; Green: Diode region where tiny current passes through the device under the application of electric field. Yellow: Red region where enough current passes through the memristors to sense the state of the device without changing its state. Red: Switching region where the memristor switches from one state to another.

oxide to the top electrode. This will cause the filament to grow since the vacancies start to drift through the most favorable diffusion paths in the presence of the electric field and hence they form a channel between the two electrodes. Once such highly conductive channels are formed, the device is in Low Resistance State (LRS) and considered as ON [10].

The onset of the figure is illustrating the I-V characteristics of the memristors which exhibits an inherent memory with a "pinched hysteresis" which can be used for information storage. For example, in the case of resistive memory RRAM, by assigning LRS="1" and HRS="0", or in the case of analog memristors, a spectrum of resistive values ranging from a HRS to a LRS.

The I-V characteristic of memristors have 3 main operating regions which are highlighted in Figure II-2. The green region in the middle is called a "diode region" where the device acts like a reverse biased diode. In the diode region, there is very little current passing by for the voltage being applied across the device. The region shown in yellow is the "read region" in which the state of the device can be read without changing or disturbing its value, since the


Figure II-3 Standard memory architecture.

voltage is not high enough to surpass the device threshold for switching. The voltage range in the yellow region is "read voltage" which is applied across the device and by sensing the current passing through, the resistance of the memristor can be measured. The region illustrated in Red in Figure II-2 is where the device switches to the other state. This "write region" consists of voltage levels which are greater than the threshold voltage of the device and hence are strong enough to move the dopants and change its resistance.

These three main operating regions provide a design tool in order to use these devices as memory elements and perform the desired operation on them.

# 2.2 Memristors as Memory Elements

As a first step in using memristors as memory elements we can think of replacing them with conventional memory elements in standard memory platforms. Figure II-3 shows such platform in which each memory device has an access transistor in series and a certain address



Figure II-4 1T-1R architecture. Memristors are accessed through selecting the series transistor.

in the array accessible by its row and the column. The address is fed serially to the array, the row and the column are decoded and the desired operation (read/write) is performed.

Replacing these memory devices with memristors, we end up with an architecture dubbed "1T-1R", shown in Figure II-4, which consists of one resistive memory in series with one access transistor at each row and column.

However, having a series transistor defeats the purpose of using these nano-devices for high-density packing of the memory since for each memory element, the limitation is still the size of the transistor. Moreover, the current needed for switching of these devices, depending on the range of the memristor can range anywhere from 10s of  $\mu$ As to 10s of mAs which applies a constraint on the size required for the series transistor having to be able to drive the required current for switching of its corresponding memristor. So can we somehow remove the access transistor? The problem raised by doing so is addressability of the memory elements. The reason why the transistor is addressable is because it's a 3 terminal device; However, by removing the access transistor we are now left with a completely resistive array which is called



Figure II-5 Crossbar memristor array with selected bits for reading and writing [11].

the "crossbar array". The crossbar array can be implemented using 2 perpendicular layers of parallel nanowires where a memristor is formed at each cross section. In the following section I will explain how crossbar arrays can be used to replace conventional memory for a highly dense memory array.

#### 2.2.1 Crossbar

As was discussed in the previous section, in order to gain from the density of memristors, cross bar arrays are used, however, their use comes with challenges since the array is fully passive which I will be addressing in this section.

Selecting the devices in the crossbar array is performed through the application of appropriate voltages across the horizontal and vertical nanowire of the desired memristor. Figure II-5 illustrates this idea for the read and the write mode.

One row can be read simultaneously by applying  $V_r$ , a voltage in the read region of the memristor, on the horizontal line and pinning the other side, the vertical line, to zero and reading off the current using a trans-impedance amplifier. To program an individual memristor to a HRS ("0") or to a LRS ("1") -V<sub>w</sub> or V<sub>w</sub> should be applied across the memristor



Figure II-6 CMOS Level Chip Architecture [11].

respectively. However, having  $V_w$  on one side and 0 on the other side, will cause unwanted memory elements to get programmed which is undesirable. In order to solve that problem, to program a certain memristor,  $V_w/2$  is applied to one side and  $-V_w/2$  is applied to the other side. This way, the non-selected devices have half of the  $V_w$  across them which is designed to lie in the read region and therefore it does not cause a state change in the device [11].

Figure II-6 depicts the CMOS level chip architecture to support the crossbar array. 3 level muxes at row and column are used to determine the read/write mode, the row/column select and Write 0 or Write 1 for the write mode. By choosing these 3 bits, desired operation is done on the desired memristors.

Overall, the memristor-based crossbar network structure can offer the following advantages: 1) it allows ultra-high density memory storage with relatively small number of control electrodes: n2 cross-points can be accessed by n-rows and n-columns in the crossbar; 2) it offers large connectivity between devices; and each column or row is connected to n-rows or columns through n different devices. However, a new challenge rises as the size of the



Figure II-7 Cutting large crossbars into many small ones. Decoding the crossbar is equivalent to decoding a "blue pin" and decoding a memristor within that mini crossbar is equivalent to decoding a "red pin". Every combination of red and blue chooses a unique memristor.

crossbars gets larger and larger since the parasitic resistance of the nano-wire becomes comparable to the memristance and the applied voltages to the crossbars will drop across the parasitic resistance instead of the memory device. Moreover, the speed of the write or read deteriorates a lot because of the large capacitances on the nanowire caused by the large size of the crossbar. In the next section of this chapter I introduce CMOL architecture which tackles this problem to enable high density 3D memory in CMOS chips.

#### 2.2.2 CMOL Architecture

CMOL architecture was first introduced by Strukov. et al in [12] as a solution for densely packing memristive devices on top of CMOS chips and I'll be explaining it from my own point of view in this section.

As I mentioned before, the problem with large crossbars becomes the undesired parasitic on the nano-wires. Therefore, instead of having a large crossbar we could instead use multiple smaller crossbars. This idea is shown in Figure II-7. In order to address an individual device, one row and column is required to address the crossbar in which the device is located in, and one row and column is required to address the device within the crossbar. Therefore, a double



Figure II-8 CMOL architecture consists of reds and blue pins in an area distributed interface.

decoding scheme is asked for in order to access the device. In CMOL terminology, we call addressing the crossbar, selecting the "blue pin" and selecting the device inside the crossbar, decoding the "red pin".

If these red and blue pins are distributed in the CMOS surface, we end up with an area distributed interface as is shown in Figure II-8 .Addressing each blue pin will select an area of crossbars and addressing the red pin within that region selects the desired device. Each square containing one blue and one red pin is a "CMOS Cell" which contains the supporting CMOS circuitry for addressing the memristive devices. The red and the blue pin are the interface connecting the underlying CMOS to the integrated top and bottom crossbar nanowires, respectively.

This seems to be solving all the problems, however, if the crossbars are fabricated in a Manhattan grid fashion, the pitch between the crossbars are dictated by the CMOS cells pitch which is much larger than the memristive nano-size and it defeats the purpose of employing memristors. Therefore, in order to exploit the intrinsic nanoscale dimensions of memristors, decoupling the underlying CMOS feature size from the device is required. One method of



Figure II-9 Every red and blue pins are embraced inside a CMOS Cell. Every CMOS Cell is connected to a neighborhood of CMOS Cells thorough a mini-crossbar. This is shown in pink in this figure and is dubbed the connectivity domain of the CMOS Cell shown in gray.

decoupling is to rotate the nanowires. Such rotation ensures that a shift by one nanowire corresponds to the shift from one interface pin to the next one (in the next row of similar pins), while a shift by r nanowires leads to the next pin in the same rows (Figure II-9). The bottom nanowires are passed through blue pins and the perpendicular top nanowires are passed through red pins. At the cross-point of these nanowires memristors are formed which are addressable through the red and the blue pin connecting to its corresponding nanowires. This is demonstrated in Figure 2.9. The colored region highlights the crossbar selected by addressing the blue pin shown with a larger blue circle. The CMOS cell containing this blue pin is connected to all the CMOS cells in the highlighted region through the memristive cross points inside this region. Therefore, the colored area is the "connectivity domain" of the selected CMOS cell. The device marked by X inside the colored region can be selected by addressing its corresponding red pin illustrated with the large red circle in Figure II-9.

CMOL tackles fabrication issues such as interlayer alignment accuracy and integration of nanoscale devices over a CMOS sub-system with larger scale feature size. Moreover, it provides high- density memory with less parasitics by sharing select circuitry between multiple memristors (1T-1R vs 1T-NR).

How can we use this architecture in order to design functional memory arrays? This is the question I will be answering in the next chapter by describing the CMOS memory platform we designed in CMOL architecture for 3D memristor integration.

# III. Chapter 3: Memory Access controller for Memristor Applications (MAMA) Chip

With this vision of a monolithic, 3D-integrated CMOL memory platform in mind, we have designed and tested the first prototype of the CMOL architecture complete with integrated memristors. This chapter focuses on the challenges involved from a circuit design perspective and the steps taken to support memristors with different ranges of resistance, threshold voltages, on/off ratio etc. More in-depth analysis of the architectural trade-offs can be found in [13] and details of the memristor integration is discussed in [14].

The plethora of memristive device designs, each with their unique advantages, requires a flexible supporting circuit architecture. The circuit design is strongly influenced by the connectivity imposed by the area-distributed interface and also the chip architecture which is designed to reflect the CMOL idea. We term this versatile chip the Memory Access controller for Memristor Applications (MAMA). A key circuit requirement for the MAMA chip is the ability to handle memristors with different  $R_{on}/R_{off}$  values, and provide the appropriate write and read voltages. This chapter explains the configurable architecture and circuits designed as a platform for integrating different kinds of memristors.

# 3.1 Chip Architecture

The chip consists of an array of CMOS cells, double decoders, programming drivers and sensing circuitry shown in blocks in Figure III-1 a. Each CMOS cell houses select circuitry including Red and Blue pins required by the area-distributed interface (Figure III-1 b).



Figure III-1 a) Overall chip architecture. b) CMOS cell. When the transmission gates are selected by Red/Blue enable signals, they connect the Red/Blue lines to the Red/Blue pins which are the interface to the integrated memristors. c,d) Blue and Red line drivers which places the appropriate voltages on the Red/Blue lines [15].

Selecting two of these Red and Blue pins accesses two of the segmented nanowires and hence a unique memristive device at the cross-point. A row-column decoder in turn accesses these pins. Thus it requires a double decoding scheme. The double decoders surround the CMOS cell array and have their function split among the Blue/Red row/column decoders. Depending on the desired operation (Read/Write) the Blue/Red line drivers place appropriate voltages on the Red and Blue lines (*Figure III-1*. c,d) which connects to the Red/Blue pins through the CMOS Cell select circuitry (*Figure III-1* b). For example, during the read operation, V<sub>r</sub> is applied across the desired memory cell and the sensing circuitry makes a binary decision regarding the memristor state and the data is shifted out serially. In the following sections the details of the circuitry in these blocks are described.

# 3.2 Writing Circuitry (CMOS Cell Design)

To write on a particular memristor, the device is addressed and the appropriate write voltages are applied across it. This is done through CMOS cells shown in Figure III-1 b. It includes two transmission gates controlled by Blue/Red enable signals routed from the double decoder. When the gates are asserted, they drive the Red and Blue pins with the appropriate



Figure III-2 CMOS cell layout. Metal 3 is used as the interface with integrated memristors. This cell occupies an area of  $32 \times 32 \mu m2$  in a 0.5 $\mu m$  process.

voltages on the Blue/Red lines. De-assertion connects the pins to a default voltage,  $V_d$ , in order to avoid floating problems such as leakage or unpredictable state-changes due to unwanted noise sources.

The transmission gates together with the memristors comprise a voltage divider. To ensure the memristor's operation in the desired region (i.e. the write region), the voltage drop across the transmission gates must be negligible. Therefore, these pass gates need to be sized accordingly.

However, the size of the transmission gates imposes a limitation on the number of CMOS Cells which can fit in the chip and hence the size of the memory supported by the chip. As a result, there is a trade-off between the maximum current drive and the size of the integrated memory on the chip.

Given these constraints, a size of W/L= $42\mu$ m/0.6µm in 0.5 µm process is chosen for the pass gate transistors. The maximum current supported by these transmission gates for a range of input voltages is reported in the next section. This maximum current can be considered as the compliance current limiting the current passing through the memristors and hence

preventing device break down [9]. Depending on the required write voltage, the minimum resistance supported by the chip can be calculated.



Figure III-3 Sensing circuitry. a) The current-sensing scheme. The memristor's current from the crossbar is compared against a reference current by the winner-take-all (WTA) circuit. b) A tunable reference current. The current can be changed by tuning the Roff-chip.

Layout realization of a CMOS cell is shown in Figure III-2. Since this CMOS chip needs to be post-processed for 3D memristor integration, the last metal layer in the On-Semi 0.5 $\mu$ m process (Metal 3) is crucial to the area-distributed interface. General power and ground routing cannot be done on this metal layer as it risks exposing and damaging these lines, therefore they are routed in Metal 2. The size of the pins comprising this area-distributed interface has been intentionally made large (24×8  $\mu$ m<sup>2</sup>) to reduce the effect of cumulative alignment error.

### 3.3 Sensing Circuitry

In order to make a binary decision regarding the memristor state, a current-sensing scheme is chosen over a voltage-sensing counterpart. In a conventional voltage-sensing scheme, a transimpedence amplifier (TIA) is utilized to convert the signal into a voltage which is then compared against a threshold voltage. However, the TIA needs at least a two stage op-amp with an appropriate output stage in order to drive the resistive load. Moreover, for a high resistive gain of the TIA, a large feedback resistor is needed, which takes up a large silicon area. Therefore, for a more compact design, the current-sensing scheme is utilized. Also, a current-sensing scheme has the advantage of a much larger dynamic range, which is required for the configurability.

Figure III-3 a shows the schematic of the current-sensing circuitry. The current drawn by the device in response to a small read voltage,  $V_r$ , is compared against a reference current. The read voltage should be picked in a region where the memristor's state does not change. This read voltage is applied by pinning one terminal of the memristor of interest to the default voltage,  $V_d$ , by an op-amp, while the other terminal is driven by the blue line driver to  $V_d+V_r$ . This read current is then compared against a reference current using a winner-take-all (WTA) circuit.

As the sensing circuitry is only connected to the memristors when the Read En signal is asserted, the pinning loop is not always closed. In order to avoid the settling time of the loop when the Read En signal asserts, a very small Ioff current (50 pA, through pbiasdifsr and pcasdifsr generated from a current diffuser) is passing through M1 while Read En is not active. As soon as Read En is activated, the Ioff current is steered to an alternate path and is drained by M2.

In order to make the sensing circuitry compatible with different memristor types (e.g. different Ron and Roff values), a tunable reference current is designed. As is shown in Figure III-3 b, this current reference can be tuned by two knobs: the off-chip resistor and the DAC output voltage across that resistor. A flexible platform for generating the read and write voltages is designed on the PCB test board by using DAC-controlled voltage sources.

26

# **3.4 Measurement Results**



Figure III-4 a) Chip micrograph. Different parts of the chip are shown. b) Individual devices integrated on the chip.

The chip micrograph is shown in Figure III-4 a. It occupies an area of  $2\times 2 \text{ mm}^2$  and was fabricated in On-Semi 3M2P 0.5µm technology through the MOSIS service. This area can potentially support 1kb of memory. Using an advanced CMOS technology node will allow for a larger memory size and smaller CMOS cell size. The range of voltages required for different

memristor types coupled with the fabrication cost make 0.5µm technology ideal for this multipurpose chip.

In order to test the functionality of the chip independent of successful memristor integration, the last row of the CMOS cell arrays is connected to peripheral bond pads. We used a potentiometer connected to two of these pads to verify the functionality of the chip over a large range of resistances, since a memristor is essentially a resistor in steady state. The PC board designed for testing the chip is shown in Figure III-5. On the right DAC voltages are configured using an FPGA in order to configure the writing and read voltage of the memristors. Digital inputs are given through the connectors on both sides of the chip controlled by the FPGA. The experimental characterization of the chip along with the memristor integration results are reported in this section.





Figure III-6 a) Write circuitry characterization. As the resistive load decreases, the writing voltage drop across the load also decreases. b) Read circuitry characterization. The reference current to the WTA is tuned by two orders of magnitude and the response of the read circuitry is plotted. The highlighted region shows the forbidden zone. c)A checkerboard pattern is used to program an array of 8x8 devices. The devices with the X,s are either shorted or failed to get programmed.

#### 3.4.1 Writing Circuitry Characterization

The most important factor of the MAMA chip writing circuitry is the maximum current drive for the various memristive loads. As is explained in section 3.2, decreasing the load resistance lowers the voltage drop across the memristor, which limits the current drive. Figure III-6 a. reports the voltage across a large range of load resistances for different writing voltages. The highlighted region (below  $2k\Omega$ ) shows the memristor range not supported by this chip since the voltage drop across the transmission gates becomes dominant. Table 3.1 depicts the maximum current provided by the chip in the writing mode for a 10% drop of the writing voltages.

| Writing Voltage (V) | 1  | 2   | 3   | 4   | 5   |
|---------------------|----|-----|-----|-----|-----|
| Current (µA)        | 90 | 178 | 183 | 213 | 260 |

Table 3.1. Maximum current in the writing mode for a 10% drop of the writing voltage across the gates.

#### 3.4.2 Sensing Circuitry Characterization

To characterize the sensing circuitry, a read voltage of 0.8V is applied across the varying load resistances. The generated current is then compared to the tunable reference current varying from 40nA to  $4\mu$ A and the measurement results are shown in Figure III-6 b. The highlighted region illustrates the forbidden zone in which the winner-takes-all comparator is in the metastable state. As a result, fluctuations on the chip can affect the output state, giving it a probabilistic nature which can be seen in the forbidden zone. The forbidden zone can be defined as a region between a maximum low resistance (RIL) and a minimum high resistance (RIH). A curve is fit to the data and the relationship between RIL, RIH and I<sub>ref</sub> in this chip is as follows:

$$R_{IH} = 1.82 I_{ref}^{-0.9375} + \frac{1}{50 I_{ref}}$$
$$R_{IL} = 1.82 I_{ref}^{-0.9375} - \frac{1}{50 I_{ref}}$$



Figure III-7 3D-integrated memristors on top of MAMA chip. on the left, Pt/Al<sub>2</sub>O<sub>3</sub>/TiO<sub>2</sub>/Ti/Pt memristors are used from Prof. Strukov's group. On the right, there are Pd/WO<sub>x</sub>/W memristors fabricated by Prof. Lu's group.

#### 3.4.3 Memristor Characterization Results

Ag/SiO<sub>2</sub>/Pt memristors are 3D-integrated on the chip [14] and are shown in Figure III-4 b. These integrated devices, once addressed, are programmed with 500ms, 5V pulses. To verify the programming, a 10ms pulse of 0.8V is applied to read the device's state. Figure III-6 c shows the checker board pattern created from an array of 8×8 devices after a program and a read pulse. Black squares represent the devices in the low resistive state. Each row of the pattern (8 bit) is programmed in parallel and read out serially. The squares with an "X" mark show the memristors which are either shorted or do not get programmed because of the fabrication yield.

Other collaborators on the MURI project have also integrated their memristors on the MAMA chip. The micrograph of these 3D integrated memristors are shown in Figure III-6 [15].

After successful integration of memristors on MAMA chip, we can move forward to investigate how these nano devices can be used as synapses in neuromorphic chips which is the subject of the next chapter.

# IV. Chapter 4: Spiking CMOS Neurons Chip

Memristors, as described in the previous chapters, are a very good candidate for an artificial synapse in neuromorphic chips: They are analog non-volatile memories which are of nano feature size and can be 3D integrated on CMOS chips. Moreover, their resistance changes based on the field applied across them. These are all ideal properties for an artificial synapse. However, designing supporting circuitry to employ them as synapse in a neural network has its own challenges. In this chapter I'm going to address these challenges by discussing how configurable circuits are employed to tackle the issues rising up by utilizing a crossbar synapses in an array of neurons.

# 4.1 Network Architecture

Let us imagine a very simple neural network where a set of input neurons are connected to a set of output neurons through memristors in a crossbar array as is illustrated in Figure IV-1.



Figure IV-1 Neural Network Architecture. Red circles represent the input neurons while the blue represent the output neurons. Neurons are modeled with a simple leaky integrate and fire model.



Figure IV-2 Applying competition between neurons by lateral inhibition.

Some of the neurons spike given a vector of analog values at the input. The generated spikes travel down the horizontal line through memristors and to the output neurons at the bottom. Depending on the value of the memristor's state, some of the output neurons fire and the generated spikes can be utilized to do useful computation in a way that each spike means a unique outcome from the network. If we employ an unsupervised learning algorithm such as competitive learning by utilizing mechanisms such as Winner-Takes-All (WTA), we can train the network to repeat such behavior. WTA enforces competition between neurons in the way which the neuron with the highest activation stays active while other neurons shut down. I explain such mechanisms more in depth in chapter 5. One way to implement WTA in such networks is to use lateral inhibition as is shown in Figure IV-2. The first neuron to spike will inhibit all the other neurons and will be the only neuron responding to that specific input pattern.



Figure IV-3 Spike Timing Dependent Plasticity as the learning mechanism observed in the brain.

In order to encourage this firing pattern in a way that the network learns to do this computation every time this set of inputs are presented, the causal relationship between the firing input and output neurons should be strengthened. This can be done through increasing the synaptic strength between the neurons which fired together and decrease the connection strength between the set of neurons at the input and the output which did not have any correlation in their firing. This is very much in accordance with the Hebb's postulate on learning: "Neurons who fire together, wire together ".

In order to apply this learning rule and keep the high-density characteristic of memristors, we need to find a way of addressing the corresponding memristors and programming them without using of a series transistor. Inspiration from learning in the brain gives us a solution to this problem.

# 4.2 Spike Timing Dependent Plasticity (STDP)

Spike Timing Dependent Plasticity (STDP) is a biological learning mechanism found to exist in the brain [16]. The synaptic strength changes as a result of relative timing of spikes between the pre and post-synaptic neurons. The weights undergo Long Term Potentiation (LTP) and strengthen if the pre and post-synaptic neurons both depolarize and fire



Figure IV-4 Membrane voltage waveforms. Pre-and post-synaptic membrane voltages for the situations of positive ΔT (A) and negative ΔT (B). Figure is taken from [18].

simultaneously. Conversely, the connection between neurons weaken when there is uncorrelated firing between the post-synaptic and pre-synaptic neuron, termed Long Term Depression (LTD). (Figure IV-3).

Previous works have demonstrated memristors as a good candidate for mimicking this learning mechanism (STDP) in the brain [17]. The question we need to answer remains: how can we employ STDP to change memristors' state in one step without the need for the series transistor?

One solution to this problem was proposed by Zamarreno-Ramos et al, in [18] in which the post-synaptic and pre-synaptic pulse shapes are engineered so that depending on the relative timing of the pre and post synaptic spike, the voltage drop across the synapse (memristor) will differ and hence they can be designed to perform STDP as desired. Figure IV-4 explains this idea.

If  $\Delta T = t_{pre}-t_{post} > 0$  the difference between the pre and the post voltages across the memristor will be higher than the threshold and therefore the connection gets strengthen. On the contrary, if  $\Delta T < 0$ , because of the pulse shape design, the voltage difference will be less than -Vth and the state of the memristor will decrease and the connection weakens. Prezioso



Figure IV-5 Generating STDP window by engineering the pulse shape across the memristors in the crossbar. a) memristor corssbar array. b) pulse shapes engineered to enforce STDP across the desired memristor. c) Voltage drop across the memristor as a function of the difference in arrival time of the pre and post synaptic neurons. D) STDP window generated as a result of the experiment. Figures taken from [19].

et al in [19] used this idea for engineering pulse shapes to perform STDP on  $Al_2O_3/TiO_{2-x}$  memristors in the crossbar shown in Figure IV-5 a. The results of the experiment are depicted in Figure IV-5 b-d. The STDP window is imitated by using pulse shape of the form shown in Figure IV-5 d.

Utilizing the results of these experiments, we designed a chip to generate these specific pulse shapes given the inputs at the crossbar.

# 4.3 CMOS Spiking Neurons (CSN) Chip

In a collaborative attempt, memristor's characteristics mentioned in the previous section was used to design a CMOS neurons array which generated pulses of the forms shown in the experiment in Figure 4.5. These memristors have the following characteristics:

- Vth+=1V, Vth-=-1V
- After forming:
  - Min Res  $\approx 10 \text{ k}\Omega (100 \mu \text{A at } 1\text{V})$
  - Max Res $\approx$  100 k $\Omega$  (10  $\mu$ A at 1V)



Figure IV-6 Characteristics of the memristors used for the Spiking Neuron Chip design. Figure is adopted from [20].

The details about the characteristics of these memristors are reported in [20] and Figure IV-6 illustrates the characteristics from [20] adopted below:

Employing these memristors in the form of a crossbar array as synapses in the CSN chip enforces some constraints on the design of the circuits. In particular, the design has to reflect on the following points:

- Design of Leaky Integrate and Fire neurons with specific pulse shapes.
- Pulse shapes need to be configurable for experimental purposes.
- Neuron's parameter needs to be configurable for experimental purposes.
- Pulses need to be able to drive the resistive crossbar array for programming purposes.
- Neuron needs to sink the current from the resistive crossbar array.

In the remainder of the chapter I explain how I address each of these constraints by designing the appropriate circuitry.



Figure IV-7 Complete neuron's model with feedforward and feedback pulse shapers.

#### 4.3.1 Neuron's Design

There are 3 main blocks in the design of the neuron, each of which addresses one of the constraint I talked about in the previous section. Figure IV-7 depicts these blocks.

The current from the crossbar gets integrated into the neuron which is designed with a Leaky Integrate and Fire (LIF) model and generates a spike upon reaching its threshold. The spike goes to the feedforward pulse generator as well as the feedback pulse generator. The former propagates into the next layer while the latter places a spike, of the shape shown in Figure IV-7, back on the crossbar changing corresponding memristors' states accordingly. There are configurable parameters incorporated in each block in order to gain flexibility on the chip. These configurable parameters are explained in details in the following sections.

#### 4.3.1.1 Leaky Integrate and Fire Neuron

Figure IV-8 illustrates the design of the leaky integrate and fire neuron (LIF). The voltage received at the input of the horizontal lines at the crossbar is converted to a current by pinning



Figure IV-8 Leaky integrate and fire neuron (1).

the vertical side of the crossbar to a fixed voltage (in this case ground). This current is then integrated in the feedback capacitor (10 pF) which leaks through the programmable PMOS current source in parallel with it. As soon as the voltage at the output of the integrator goes below a certain  $V_{th}$ , the comparator flips to a high voltage which resets the integrator and triggers the feedback pulse shaper. S1 switches to the "spike mode" where it connects the positive input of the op-amp to the output of the pulse shaper. The high gain op-amp copies the pulse shaper output to its negative terminal and hence to the vertical nanowire in the crossbar. Depending on the relative timing of the pulse presented at the horizontal line and the output pulse generated at the vertical line, the voltage across the memristors varies and the memristors are therefore programmed accordingly. The threshold voltage of the neuron is connected through a resistor directly to an I/O pad in order to gain control over the neuron's firing.

This op-amp leaky integrator along with the comparator is the core of the LIF neuron. However, there are some constraints enforced by the architecture which should be designed carefully:



Figure IV-9 Leaky integrate and fire neuron (2)

The integrator I just explained contains a capacitor in the feedback loop of the op-amp and hence opens the feedback loop in DC operating mode. In order to get around that problem a high value resistor in the form of a "pseudo resistor" [21] is added in parallel with the capacitor. (Figure IV-9)

Moreover, lets us imagine a scenario where one input is applied at the horizontal line and because of the state of the memristors is not able to trigger a spike in the neuron. The charge accumulated at the integrator should be kept intact for the next input, since the information about the previous input is important to be kept for certain applications such as coincidence detection. However, since the input pulse is bipolar and takes negative values and the vertical side of the crossbar is grounded, there is a current flowing in the opposite direction towards the input which needs to be sourced through the op-amp. As a result of that, the capacitor would lose its information. One solution to that is to employ the diodes as shown in Figure IV-9. If the op-amp needs to support current for the crossbar, the current takes the path with the diode D1 in parallel with the capacitor and diode D2 protects the charge in the capacitor.



Figure IV-10 Complete leaky integrate and fire model.

Additionally, in another scenario we can imagine the memristors being in LRS and as a result of that any input can easily trigger the neuron which is not desirable since frequent firing of the neuron does not contain any information (it happens for any input!) and is reducing the entropy. Therefore, we employ a "draining path" right at the input of the integrator to drain the current out of the crossbar and reduce the amount of current going to the integrator. The draining current source is designed configurable in order to add control for the amount of current going to the neuron. (Figure IV-10)



Figure IV-11 OpAmp topology employed for the integrator in the LIF neuron. The OpAmp has an extended common mode range at the input with a class A-B push pull at the output to drive the memristive crossbar array.

Also, as I mentioned in the beginning of the chapter, a competitive learning approach is taken toward training this hardware based neural network. This approach is enabled through employing Winner-Takes-All (WTA) by utilizing lateral inhibition [22]. If a spike is emitted from each of the neurons in the network the signal "global inhibition" is received by all the neurons and resets their state through the transmission gate illustrated in Figure IV-10.

In the aforementioned scenarios for the state of the inputs, memristors and outputs, I have explained certain constraints which the op-amp needs to reflect upon: High-gain, high output drive and high input and output swing. Figure IV-11 shows the op-amp topology I used in order to satisfy these constraints.

By placing two complementary (NMOS, PMOS) differential pairs in parallel as is depicted in Figure IV-11, an extended common mode at the input is achieved. When the input pulse



Figure IV-12 Amplifier stay stable for more than 2 orders of magnitude to support the current needed to program the memristors in the crossbar array.

changes from a positive to a negative value, the NMOS pair start to turn off and the PMOS transistors start conducting and exchange their functionality at the input stage and vice versa. Hence the gain of the op-amp does not drop as one pair of the transistors turn off. When the input voltage is within a range which can make both pairs on, its total trans-conductance will be twice of that when only either pair is on and that will double the gain. However, that is not of our concern in this design since our constraints is to keep the loop closed by having a high enough gain. The gain of the op-amp at the typical-typical (tt) corner and with the common mode voltage tied to ground is 91 dB.

An output stage that exhibits a large output swing, together with a low quiescent power consumption, requires a common- source-type class A-B output stage as is shown in Figure IV-11. Such an output stage, however, needs to be compensated in order to stabilize the amplifier since the output node shows a high-impedance character [23]. The compensation is done by adding a zero to the transfer function through R1 and C1. R1 and C1 have to be chosen so that the op-amp stays stable with the change in the resistive load as a result of memristors' state change. In our case, R1 is an HPoly with a value of 10k ohms and C is a MIM capacitor



Figure IV-13 Desired pulse shape with configurable parameters.

with a value of 1 pF. The corner simulations are done thoroughly to ensure the stability with the change of C and R in different corners.

Figure IV-12 show the simulation results of the LIF neuron in response to an input shown in blue in Figure IV-12a. the spike gets emitted from the neuron and the appropriate pulse shape is generated. The op-amp stays stable for over more than two orders of magnitude of change of the load and supports the current needed to program the memristors. This is shown in Figure IV-12 b.

#### 4.4.1.2 Feedback/ Feedforward Pulse Shaper

The desired feedback pulse shape, as we have seen in section 4.2 and is also shown in Figure IV-13 is a square pulse with 3 voltage levels:  $V_H$ ,  $V_L$  and  $V_M = V_{pin}$  (=gnd in our design) and pulse widths of PW<sub>1</sub>, PW<sub>2</sub> as is illustrated in Figure IV-13.

Cycle to cycle and batch to batch variation of the memristive crossbars asks for a configurable pulse generator whose characteristics can be controlled. The pulse generator and the configurability is designed into the chip through DAC voltages and clocks as is shown in Figure IV-14.



Figure IV-14 pulse shaper design. Configurability is enabled through the use of DACs and clks.

The shaper block consists of two half-shaper blocks each of which shapes half of the pulse (top/bottom). The spike is first received by the top half shaper, is passed through the SR latch and therefore is kept high. The transmission gate T1 hence starts conducting *DAC1* voltage to the output node. The SR output also enables the 10-bit counter C1 to start counting *clk1* and when the  $10^{\text{th}}$  bit goes high, the counter is reset and so is the SR latch at the input. Upon resetting the SR latch two events occur:

1) T1 stops conducting and therefore the voltage at the output drops. The time it takes for C1 to count *clk1* up to 512 (to flip the  $10^{\text{th}}$  bit) determines the length of PW<sub>1</sub>.

2) Since flipping Q10 resets the counter and the SR latch, a narrow spike, much like the neuron's spike, gets generated. This spike triggers the second half shaper in which the same series of events from the top half unfolds. *DAC2* and *clk2* control the pulse shape and voltage level of the bottom half-shaper independently of the top one.

Figure IV-15 depicts the simulation results showing the configurability of the pulse shape. DAC1 and DAC2 voltages tune  $V_H$  and  $V_L$  and clock frequency of *clk1* and *clk2* control PW<sub>1</sub> and PW<sub>2</sub> independently.



Figure IV-15 Spectre simulation results illustrating the configurability of the pulse shape through DAC (left) and clk (right).

The complete neuron layout containing the LIF and the feedback and the feedforward pulse shapers is shown in Figure IV-16. The layout is designed to be tiled in an array of 5x5 neurons. The blue and red pins shown in the figure are designed as the CMOL architecture platform for the possible memristive crossbar 3D integration on top of this chip. Last metal layer (Metal 6) is used for the design of these pins. The red pin is connected to the input of the integrator and the blue pin gets input from the previous neural layer or an external source. In the CMOL architecture as I have explained in the previous chapter, each neuron plays the role of the CMOS cell which will be connected to the adjacent neurons through its "connectivity domain".



Figure IV-16 Complete layout of the LIF neuron with feedforward and feedback pulse shapers. Red and Blue pins are placed to enable CMOL implementation of memristors for 3D integration.

#### 4.3.2 Inhibition Network

Training the network requires employing a form of unsupervised learning and as I explained in section 4.3.1 competitive learning algorithm is used for training these spiking neurons on chip. Winner-Takes-All (WTA) mechanism in the form of lateral inhibition between neurons is an efficient solution for utilizing such learning algorithm. The inhibition network is a simple OR gate which takes input from all the neurons' outputs and gets routed to all the neuron's inputs. Each neuron who fires will rise the OR gate output and shut down all the other neurons' activity. This block is essentially in a feedback loop from the output of all the neurons to all of their inputs. Since the neurons are going to be structured in an array form, the layout of this block has to be designed carefully. Figure IV-17 illustrates the design and the layout of the inhibition block. There are 25 neurons in the array, therefore the OR gate has a fan-in of 25. This OR gate is divided into 5 NOR gates who feed into a NAND gate. The

| *                    |                         |            |      | <b>1</b> 38 |
|----------------------|-------------------------|------------|------|-------------|
|                      |                         |            |      |             |
|                      |                         | national - |      |             |
|                      |                         |            |      |             |
| i<br>b               |                         |            | 1221 |             |
| i <b>Keria.</b><br>t | ₩ <b>₩</b> ₩ <b>₩</b> ₩ |            |      |             |
| i <b>Fest</b>        |                         |            |      |             |
| n                    |                         |            |      |             |
|                      |                         |            |      |             |
|                      |                         |            |      |             |

Figure IV-18 Complete layout of the LIF neurons 5x5 array. Each neuron takes an area of 500 x 500  $\mu$ m<sup>2</sup>.

25 neurons are placed in a 5x5 array and hence each row of the array contains 5 neurons which feed the NOR gate in their proximity. The layout of this block is therefore a long narrow rectangle placing each NOR gate close to its row. The inverters are sized accordingly in order to drive the input gates at the neurons.

#### 4.3.3 Neural Array

The neuron block is tiled in a 5x5 array as is depicted in Figure IV-18. Each neuron cell



Figure IV-17 Inhibition block schematic (left). Layout of one of the 5 sections (right).

has an area of  $500\mu m \ x \ 500\mu m$  and the whole array takes 2.5 mm<sup>2</sup> of the chip. Last two metal



Figure IV-19 Chip Micrograph in Silterra 180 nm.

layers are used to route power and ground and the CMOL area distributed interface. Threshold voltage, integrator leak parameter and the "current drain" parameters are controlled by the I/O pins and are common between the neurons.

The chip micrograph is shown in Figure IV-19. The chip is designed in Silterra 180 nm and takes 5 mm x 5 mm of silicon area. The highlighted squares on the left side of the array are MIM caps which are placed to satisfy the DRC requirements of the technology.

For characterization purposes a stand-alone neuron is placed on the bottom left of the chip and all its controllable parameters are routed to the I/O pins. CMOL platform with the area distributed interface is visible since the last metal layer was chosen for that and one "CMOS Cell" is highlighted in yellow.

The chip is being wirebonded and will be tested upon packaging.
# V. Chapter 5: Spatio-temporal Encoding Approach

So far in this thesis, I have been talking about how we can employ memristors as artificial synapses. I explained that since they are nano-scale and can be integrated on top of CMOS chips, we can use the *space* optimally to pack as many of these memory cells as possible in a certain area. This chapter starts a different approach to address the problem of connectivity between the neurons in neuromorphic chips. An approach that uses a new dimension, *time*, which we can employ to optimize the information encoding and hopefully, through that, we can reduce the number of connections needed on the chip to do neural computation.

# 5.1 Introduction

As I mentioned in the introduction, researchers have been trying to mimic the brain to perform useful computations for more than 70 years now. The original work of McCulloch and Pitts in 1943 proposed a neural network model based on a simplified model of the neurons [24]. The model of these neurons are depicted in Figure V-1. In this model, neuron sums the product of its inputs by their synaptic strength and if higher than a certain threshold, it generates a spike. As it was observed in neuroscience, the higher the input intensity of the neuron, the



Figure V-1 Simple model of the biological neurons (left). First mathematical model of the neurons (right). Figure is taken from [26].



Figure V-2 Neural pathway from the retina to the inferotemporal cortex, where visual objects are recognized. Figure taken from [36].

higher the frequency of spiking. Therefore, the first obvious assumption was that information is encoded in the rate of neural firing: Each neuron would generate a "rate of firing" and the "rate" will transfer between the neurons as a continuous floating point number.

However, this rate-based code is not very efficient because of the reasons described below:

1) Maintaining such a set of neurons is energetically expensive, as to encode a single variable many spikes need to be generated and averaged over a window of time to calculate the rate of firing.

2) Real neurons rely on pulses as an important part of information transmission from one neuron to another. So instead of transferring a "number" as a rate, real neurons communicate through single spikes which is much more energetically favorable.

3) There are very good arguments against the rate-based code, most famously from S. Thorpe and his colleagues. In [25] authors argue that there are situations where information processing in the brain is too fast to be compatible with the rate based codes. For example, in the visual cortex it takes only about 100-150 ms for complex visual stimuli such as faces or food to be recognized. This is while the visual information pathway from the retina to the last layer of the visual cortex is about 10 layers (shown in Figure V-2). Lateral Geniculate Nucleolus (LGN) receives sensory input from the retina and transfer the information through optical nerves to the cortex. In V1 features of the image will be extracted and as the information goes further in the layers, these features will combine to construct more and more complicated features until



Figure V-3 Intensity to latency conversion. The stronger the input, the faster the neuron spikes. Figure is taken from [30].

the object is recognized. Taking into account the maximum firing rate of 100 Hz for the neurons in that region of the brain, it leaves about 1 spike generation for each processing layer. Therefore, rate-based code cannot keep up with this rate of information processing.

4) Evidence from neuroscience has increasingly made it clear that information is carried in the individual action potential rather than aggregate measures such as "firing rate". Rather than the form of the action potential, it is the number and the timing of spikes that matter. In fact, it has been established that the exact timing of spikes can be a means for coding information in different parts of the brain [26].

These downsides of the rate-based codes mentioned above will bring us to the next topic: Temporal codes.

# 5.2 Temporal Codes

As was argued in the previous section, finding a way to represent information in the form of spikes is beneficial. One way of doing so is by encoding intensity in the time-to-firstspike which compares well with the traditional rate models. The more intense the input is, the



Figure V-4 Illustration of using temporal codes for computation. Time is divided into time windows and information can be encoded depending on which neurons spike in each time window. Figure is taken from [26].

earlier the spike emits. This will translate a vector of real numbers into a spike train. Figure V-3 plots the activation of the neurons versus time for the inputs with different intensity.

Using temporal codes, a Spiking Neural Network (SNN) can be designed with n input neurons N<sub>i</sub> to encode an n-dimensional input vectors containing the pattern  $x = (x_1, ..., x_n)$  which are being fed to the network at each successive temporal window (comparable to successive steps of traditional NNs computation). In each time window, a pattern x is temporally coded relative to a fixed time Tin (enforced by the rate of pattern presentation) using a single spike emission of neuron N<sub>i</sub> at time ti =Tin-xi, for all i (Figure V-4).

As we discussed in 5.1, by taking advantage of the temporal code the information of each dimension of the input can be encoded using a single spike which can be easily transferred to other neuron in the successive layers.

Due to the nature of the coding using only one spike per pattern presentation, this coding scheme is not only fast, but also power efficient. These two measures normally don't occur at the same time, meaning that higher speed of information processing translates to



Figure V-5 Possible neural codes provided by the temporal coding. Figure is taken from [37].

higher power consumption through expression  $P = \alpha V^2 f$  where  $\alpha$  is the activation factor, V is the supply voltage, and f is the frequency of operation. Therefore, being able to do the computation faster while saving on power is extremely efficient. Other than energy efficiency, and speed, temporal codes can also open up a whole new range of coding options, many of which are largely unexplored.

# 5.3 Time as Basis for Information Encoding

From a combinatorial point of view, using the time of the spikes as information representation provides a large information capacity, given a small set of spiking neurons. For instance, consider that a stimulus has been presented to a set of *N* spiking neurons each of which spiking a maximum of one spike in a certain time window. As shown in Figure V-5 information can be encoded using different schemes which are explained in detail in [25] and I will touch upon them below. For each coding scheme introduced, the information capacity is also calculated.

#### • Count Code

In this coding scheme, overall number of spikes fired by neurons in a time window are counted and each input representation will be coded using the number of the neurons which are fired in that time window. With such a coding scheme, the maximum amount of information that can be transmitted is equal to  $log_2(N+1)$  bits, where N is the number of neurons, since there are only N+1 possible states of the system.

• Binary Code

In this coding method, N bits are to encode the input vector, one bit for each neuron. If the neuron is "active" and emits a spike the corresponding bit is 1 and otherwise is zero. The N bits can also be justified by considering that since each neuron can have 2 states, the system can take  $2^{N}$  states which when applied to Shannon Theorem [27], the information capacity,  $\log_2(2^{N})$  will be N bits.

• Timing Code

Using "Timing Codes" information is encoded in the precise timing of spikes. Information encoding capacity in this case depends on the precision of determining the spike time. The more the precision the more we can distinguish between relatively close spikes and hence the more the information capacity. If we suppose that spikes can be timed with a precision of 1 ms, the maximum amount of information that could be transmitted in t ms will be N\*log<sub>2</sub>(t) bits. Such timing based codes are clearly potentially extremely powerful, but have the drawback that the decoding mechanism would need precise timing evaluations which is rather computationally expensive.

#### • Rank Order Coding (ROC)

Instead of encoding the information in the exact spike time of the neurons, Thorpe et al in [25] introduced ROC in which information is encoded in the rank of the spikes from neurons. In this coding scheme, the order of the firing between neurons will encode the input vector. For example, if we have 3 neurons A, B and C, each permutation of A, B and C will be a new code. As there are 3! =6 ways of permuting 3 objects, the code space will be:

#### {ABC, ACB, BAC, BCA, CAB, CBA}

Since there are N! states of the system at each time window for N neurons, the information capacity of ROC is log<sub>2</sub>(N!).

So far, we have seen how we can use temporal codes to increase the information capacity using a fix number of neurons, N. In comparison, timing code and ROC contain a relatively large coding capacity. In order to decode the information in the time of arrival of the spike we need a very precise timing resolution. We should also keep in mind that decoding ROC would also need precise timing since we need to distinguish between the order of spikes.

## 5.4 Rank Order Code

In order to use ROC to train neural networks, a learning algorithm is needed which reflects upon the order of neural spiking:  $\Delta W = f(order)$ . In other words, when a pattern is presented to the network of neurons, the weights of the neurons who fire earlier will change more than the ones who fire later. As a result of that, after training, the earlier spikes carry more information about the input than the later ones do.



Figure V-6 Competitive Learning- Each output neuron represents a cluster. N\_A and N\_B represent cluster A and B respectively and W<sub>A</sub> and W<sub>B</sub> are the centers of the clusters. Upon the arrival of every input pattern, the winner neuron's weights adjust themselves to get closer to the input pattern.

Now, consider a case where this coding scheme is employed in some form of unsupervised learning such as competitive learning. In the unsupervised (clustering) problem, we are given a training set  $\{x^{(1)}, \ldots, x^{(m)}\}$ , and want to group the data into a few "clusters." Classic competitive learning such as K-means clustering algorithm finds K cluster centroids that minimizes the distance between data points and the nearest centroid [28]. Simply put, at each pattern presentation, there is one cluster whose centroid's distance to the input vector is the least. The new pattern will be grouped with that cluster and a new centroid will be calculated for the cluster with the new arrangement.

In the concept of neural networks, each cluster represents a neuron and its centroid which is the mean of the cluster, is the neuron's weight vector  $\in \mathbb{R}^{n \times k}$  for an n-dimensional input vector and k clusters. Every time a new input is fed to the input neurons ( $U_1$  and  $U_2$ ) (Figure V-6), the most active output neuron is the one whose weight vector is the closest to the input vector. This algorithm is called the Winner-Takes-All (WTA) algorithm, since one neuron wins the competition between neurons and takes the input into its cluster. Winning neuron's weights adjust themselves in a way to get closer to the new input pattern and include that pattern in the cluster. In other words, weights are the running average of the input patterns.

$$W_{A}(t) = \left(\sum_{i=1}^{t} u_{i}\right) \frac{1}{t} = \left(\sum_{i=1}^{t-1} u_{i} + u_{t}\right) \frac{1}{t}$$
$$= \frac{t-1}{t} * W_{A}(t-1) + \frac{u_{t}}{t}$$
$$= W_{A}(t-1) + \frac{1}{t} (u_{t} - W_{A}(t-1))$$
$$\to \Delta W = \varepsilon (u_{t} - W)$$

where  $\varepsilon$  is the learning rate [29].

Now, let us apply K-means algorithm to Spiking Neural Networks (SNN) and specifically to Rank Order Code (ROC). Under the presentation of each input vector, there is one neuron whose weight vector is closest to the input vector resulting in the strongest input and hence the earliest spike emission. Lateral inhibition can be employed as a means to implement Winner-Takes-All such that the first spike at the output layer inhibits all the other neurons and will be the winning neuron whose weights are going to change towards the input. This way, each neuron will be trained to respond to a specific pattern. For example, in a work done by Rudy Guyonneauet al in 2004 they train 4 neurons using the rank order code in a spiking neural network to cluster 4 different images [30]. As is shown in Figure V-7, at the end of the training set they were able to get each neuron to respond to a specific image from the training set.



Figure V-7 Emergence of selective responses of each neuron to a specific pattern. Lateral inhibition is applied as a winner takes all mechanism and competitive learning results in the assignment of each pattern to the emission of one spike from one neuron. Figure is taken from [30].

Hence by using Winner-Takes-All and Rank Order Coding, 4 neurons can encode 4 images. However, as we mentioned in the previous section, 4 neurons using rank order code have the potential of encoding 4!=16 different input vectors and by applying Winner-takes-all, this coding space is being wasted and not used to its full potential.

Moreover, a greedy algorithm like WTA combined with Hebbian learning puts the system in a positive feedback loop driving the weights to one or zero which can be digitally stored. Digital weights have the advantage of being more robust and immune to noise but are losing a lot of information in digitization. However, we want to explore the true analog computation and study the power of computation using analog memory which brings us to the concept of Winners-Share-All.

### 5.5 Winners-Share-All (WSA)

Instead of forcing the network to have only one winner for each time window which wastes the code space, I propose to have multiple winners at the presentation of each input. Then the question arises: How many winners are enough? In ROC I explained that the earlier rank spikes



Figure V-8 Comparison of the number of output neurons required to recognize patterns between WTA (blue) and WSA (red) mechanism. As the number of patterns increase, the efficiency of using WSA becomes more apparent. have a lot more information about the input scene that the later ones do. So how many of them should we keep?

Let us imagine we have *n* output neurons from which *k* are firing. The total amount of information capacity of this arrangement is then  $log_2\binom{n}{k}$ . To maximize this information capacity, *k* should be n/2. Therefore, from a combinatorial point of view, if we enforce the network to fire half of its output neurons in a time window, we will increase the information capacity by:

$$\alpha = \frac{\log_2 \binom{n}{\frac{n}{2}}}{\log_2 n}.$$

To get a sense of how much increase this is, for n=10,  $\alpha$  is 2.4, for n=100  $\alpha$ = 14.5 and for n=1000  $\alpha$ =100. Thus as the number of neurons at the output grow, the increase in the information capacity becomes more apparent.



Figure V-9 The case with two similar rank codes in which only the rank of two last spikes are different.

To highlight yet another advantage of this algorithm, we can compare the number of neurons needed in order to classify P numbers of patterns with WSA vs WTA. Figure V-8 depicts this comparison. Using WTA, the number of output neurons required for classification grows linearly with the number of patterns at the input. However, using WSA, number of neurons needed undergoes a logarithmic compression and for large number of patterns the gap between the number of output neurons in WTA vs WSA algorithm increases by a lot.

Although this algorithm is providing us with a lot more information capacity, it's still lower than ROC  $(\log_2 n! \ vs \log_2 \binom{n}{k})$ . However, it should be noted that training networks with ROC is much harder than the proposed scheme. Why?

Consider the case below with 6 output neurons where there are two cases with the same order of spiking pattern except for the 5<sup>th</sup> and the 6<sup>th</sup> neuron (. Basically, in one case we have the code: 1>2>3>4>5>6 and in the other case, we have: 1>2>3>4>6>5. Although these two codes are different, they cannot be used to encode two different objects at the input. Why? Since earlier-rank neurons provide a lot more information about the patterns than the later ones do, these two rank orders are very similar and cannot be used to encode two different patterns.

In other words, the "least-significant-bits (LSBs)" don't contain much information about the input and can be ignored in the coding process. This will result in using only the "Most Significant Bits (MSBs)" or in other words, only half of the neurons which is what WSA is proposing.

In the next chapter, I will explain how this idea can be used to perform computation in the form of pattern recognition.

# VI. Chapter 6: Applying WSA to a Classification Problem

In order to show the power of this algorithm in practice, I applied it to a neural network to perform a rather small classification problem in which 14 patterns of English Alphabets are to be clustered with 6 neurons. If we were to use the Winner-Takes-All algorithm on this problem, we would need 14 neurons at the output. With Winners-Share-All, using only 6 output neurons, we should be able to classify  $\binom{6}{3}$ =20 patterns. Figure VI-1 shows the training set and the test set patterns chosen for this experiment. The set consists of images of the patterns with the size 15 pixels x 15 pixels and the last column of the training set shows the ideal, non-noisy patterns.



Figure VI-1 Training set and Test set patterns used for the classification problem.

The rest of the patterns are made by flipping 10 pixels either on the pattern or in a neighborhood

of one pixel around the pattern inside the image. The reason for generating the noisy patterns this way is because if we flip the pixels somewhere in the corner of the image, it does not perturb the pattern at all and hence is very close to the ideal image. Using this method, 5 noisy versions of each pattern are generated for training and 2 of them are made for testing in order to evaluate how well the network "generalizes". The concept of *generalizing* in machine learning is referred to how well a neural network classifies the patterns it has not seen before. A neural network that clusters the patterns well only when it has been presented with it before is only *memorizing* the patterns rather than *learning* them. Hence, it's very important to measure the accuracy of the classification done by the network using the test set.

### 6.1 Network Architecture

The network architecture used here is structured in a similar manner to hierarchical neural models, specifically to Convolutional Neural Networks (CNNs). A Convolutional Neural Network (CNN) is comprised of one or more convolutional layers (often with a subsampling step) and then followed by one or more fully connected layers as in a standard multilayer neural network. The architecture of a CNN is designed to take advantage of the 2D structure of an input image (or other 2D input such as a speech signal). This is achieved with local connections and tied weights followed by some form of pooling which results in translation invariant features. Another benefit of CNNs is that they are easier to train and have many fewer parameters than fully connected networks with the same number of hidden units [31].

Figure VI-2 shows the full neural network architecture used in this work.



Figure VI-2 Neural network architecture used in this work. Intensity is converted to time of spike in the first layer and features of the image are extracted in the second layer. The patterns are recognized at the last layer.

As in CNNs, the first neuronal layer is inspired from V1 in visual cortex which responds to orientation edges in the input scene. These edges are designed in the form of filters (kernels) in the first layer which are *convolved* with the input scene (and hence the name convolutional NN) which results in extracting the features from the image. The activation of the neurons at the first layer in response to the convolutions (extracted features) are propagated to the next layer which may or may not be a convolutional layer. In the next layers, the features combine to more and more complex features until the pattern is recognized at the last layer.

Figure VI-2 illustrates how four filters are designed to extract vertical, horizontal, 45 and 135 degree edges from the image. These (3x3) filters scan the (15x15) input images with nonoverlapping windows and the convolution results in 5x5 feature maps in the second layer. The reason why we chose to use non-overlapping windows is because the size of the image we are using (15x15) is relatively small and the overlapping windows don't contain much more information than the non-overlapping ones. The limiting factor in the size of the images is the processing power causing simulation times to be very large for larger images and hence making the process of design very tedious. Each "feature map" in the second layer contains a certain edge. The neurons on the same coordinates on the different feature maps have the same receptive field on the input image meaning they get their inputs from the same part of the image.

As is depicted in Figure VI-2, the third layer is combining the features from the second layer in a fully connected manner to recognize the images on the output layer. This layer is trained in a completely unsupervised fashion using Spike Timing Dependent Plasticity (STDP).

The spiking neural network is coded and simulated in MATLAB. Neurons and synapses are modeled mathematically and are discussed below. The rest of the details of the network will be discussed later in the chapter.

#### 6.1.1 Neuron's Model

A leaky integrate and fire model is chosen for the neurons as is defined mathematically as:

$$V_{mem}(t) = \int_{(n-1)T}^{nT} (Input_PWM(t) - \alpha V_{mem}(t))dt$$
$$n = floor(\frac{t}{T})$$

Where T is the clock period for presenting patterns and is chosen here as 10m sec.  $\alpha$  is the leak coefficient and *Input\_PWM* is the pulse width modulation of the input spikes at each layer. This modulation keeps the pulses high until the end of the window. Pulse width modulation weights the spikes who come early more than the ones who come later. As we have discussed before, in temporal codes the spikes which are emitted first contain more information



Figure VI-3 Pulse Width Modulation (PWM) of the pre synaptic input spike in order to weight the earlier spike more than the later ones. The neuron integrates the dotted green area under the PWM signals and hence the earlier signals stimulate the neurons more effectively.

about the input than the later ones. Therefore, since we are utilizing multiple spikes at each layer (WSA) we need to weight them differently based on the time of the arrival. Figure VI-3 illustrates this idea. As is shown, the neuron integrates the area under the product of the weight by the pulse width modulated input. Therefore, the earlier the spikes arrives from the previous layer, the larger the area under the curve and the more it triggers the neuron in the next layer.

At the end of the time window the pulse width modulation and the membrane potential are reset to zero and the neuron awaits the next input pattern:

$$PWM(nT) = 0$$
$$V_{mem}(nT) = 0$$
$$n = 0, 1, 2, \dots, floor\left(\frac{t}{t_{end}}\right)$$

Where  $t_{end}$  is the length of the simulation.

#### 6.1.2 Synapse Model

The connection between the neurons are modeled as a single variable whose value changes based on *dwp* (positive changes of w) and *dwn* (negative changes of w) such that:

$$w(t + dt) = w_0(t) + \beta (dwp(t) - dwn(t)) + f(.)$$

Where  $\beta$  will scale the changes of w and f(.) contains the dynamics of the synapses which will be discussed in section 6.4.

In the following sections of this chapter I will go through the details of the design choices and output of each layer.

# 6.2 Layer 1: Converting Pixel Intensity into Spikes

As I discussed before, in temporal codes each input is presented in a time window and the information about the input is converted into spike times. As is shown in Figure VI-4a, in layer 1, each neuron is assigned to a pixel whose normalized intensity is given as an input to the neuron. Pixels refresh their values every 10 ms which is the length of the time bin in which the network processes each pattern. In other words, the normalized pixel intensity is presented at the beginning of the time window and is kept constant until the end of the time window. The input images are normalized by the number of "on" pixels so that if an input pattern has intrinsically more number of black pixels than others, it will not cause stronger stimulus for the next layer and all patterns have the same total drive for the following neural layer since they are scaled by the total number of "on" pixels in the image.

Note that input patterns are shuffled randomly and then given to the input neurons every 10 milliseconds. The reason why is if the data is given in some meaningful order, this can bias the network and lead to poor convergence and generally a good method to avoid this is to randomly shuffle the data prior to each epoch of training.



Figure VI-4 First layer: converting pixel intensity to spikes. Normalized patterns are presented to the network every 10 ms and in that time window network processes these patterns. a) Each neuron is assigned to one pixel. b) Raster plot showing the spiking of 225 neurons in the simulation time. c) zoomed version of the raster plot showing the spiking of neurons in each 10ms time window in which the patterns are presented.

Raster plot in Figure VI-4b shows the spike times of the 225 neurons in the first layer. Figure VI-4c depicts the zoomed version and illustrates the firing of each neuron in every time bin (10 ms). The neurons containing a black pixel (with a white background) in the pattern presented at each time bin are the ones who emit a spike.

# 6.3 Layer 2: Extracting features from the Images

In the field of image processing appropriate filters are applied to an image in order to extract certain features from it through convolving these filters with each *patch* of the image. In the concept of neural networks, this translates to neurons whose weight vectors act as the filters and whose receptive field act as the *input patch*. As a result of that, the output of the neuron is the convolution (product of sum) of the input image patch with the filters defined by the neurons' weight vector.

The filters I have chosen at the second layer of the neural network for feature detection are vertical, horizontal, 45 and 135 degree edges. The weights (synapses) of these filters are non-



Figure VI-5 Second layer: extracting edges from each kernel. 3x3 kernels are taken from the image and are convolved with features that are hardwired in the network. This layer of neurons responds to dominant edges existing in each 3x3 kernel.

plastic and are *hardwired* in the program. As is illustrated in Figure VI-5 a, every 9 neurons from the first layer are representing a 3x3 patch from the image and connect to 4 neurons in the second layer. These 4 neurons receive spikes from the first layer and depending on the dominant features of that patch, the corresponding neurons fire. Since the image is 15 x15 and the receptive fields of each group of 4 neurons are of the size 3x3 and are non-overlapping, the second layer needs  $4 * \left(\frac{15}{3}\right) * \left(\frac{15}{3}\right) = 100$  neurons. Neurons 1-4 correspond to the left corner of the image and neurons 5-8 correspond to the window just to the right of that and so on and so forth. In each time bin of 10 ms where a new pattern is presented, spikes from the first layer travel through the second layer and the neurons corresponding to the dominant edges of that pattern spike. This can be observed in Figure VI-5 b with the highlighted time window. Figure VI-6 c depicts the raster plot of the 100 neurons in the second layer in 10000 seconds.

### 6.4 Layer 3: Classification

The third layer in this convolutional neural net is fully connected to the feature extraction layer. Our goal here is to train these connections in an unsupervised fashion to classify 14 patterns shown in Figure VI-1 using spike combinations of 6 output neurons. In this spiking neural network, Spike Timing Dependent Plasticity is used to modify weights and in this section I'll explain the details of the learning and the challenges while training this spiking neural network with Winner-Shares-All algorithm in a completely unsupervised fashion.

#### 6.4.1 Challenge 1: Learning

a) Positive Weight Change

As explained before, during each time bin, the neuron which spikes earlier carries the most amount of information about the input and in order to incorporate that in the model, I use pulse width modulation to the input spike which results in longer stimulation of post-synaptic neurons from the pre-synaptic spikes arriving earlier.

To reflect this in the learning algorithm:

- The pre-synaptic spikes arriving earlier and causing the post synaptic neuron to fire should undergo a larger weight change than the ones who helped with the stimulation but arrived later.
- ii) Moreover, I introduce an intermediate parameter C inspired by the calcium concentration and its role in learning. This value increases with the arrival of the pre-synaptic spike at the synaptic joint and decays over time in the form of  $c(t) = e^{-a(t-t_{spike})}$ . When the post-synaptic spike occurs, it samples this parameter at the time of its firing and the synaptic change will be directly proportional to this value.

Now, combining the two aforementioned ideas, the C parameter should increase in the form of  $c'(t) = 1 - e^{-a(t-t_{spike})}$  when a pre spikes happens, so that it can incorporate the effect of early versus later spikes. Therefore, the later spikes have a lower value of C in comparison with the earlier spikes and hence their corresponding weights undergo a smaller weight change. Basically, this learning algorithm is a form of anti-STDP rule within the time bin, because the weight change will be greater as the pre spike emits earlier in time (within the time bin) with respect to the post spike. This is desirable since the weight change reflects the mutual information between the pre and the post synaptic neurons which is encoded in the time of arrival of the spikes.

The learning algorithm is shown graphically in Figure VI-7a and can be described mathematically as:

$$c(t) = \int \left(\delta(t - t_{pre}) - \alpha * c(t)\right) dt$$
$$c'(t) = u(t - t_{pre}) - c(t)$$
$$dwp = L_{RateP} * \delta(t - t_{post}) * c'(t) = L_{RateP} * c'(t_{post})$$

Where dwp is the positive weight change and  $L_{RateP}$  is the positive learning rate.

#### b) Negative Weight Change

When there is no correlation between a pre-synaptic and a post-synaptic neuron the connection between them undergoes a negative weight change. This lack of correlation translates to the post-synaptic neuron firing before the pre-synaptic counterpart. The later the



Figure VI-7 Spiking learning algorithm developed for WSA. Calcium concentration models are used as part of the Anti-STDP rule to calculate dwp and dwn.

pre-synaptic neuron spikes with respect to the post synaptic neuron (within a time bin), the more uncorrelated the two neurons are. Hence, the same anti-STDP rule applies here.

Note that the weight could also endure a negative change when there is no correlation whatsoever between the pre and post; meaning that the pre-synaptic neuron does not emit any spike within the time bin while the post has spiked. In that case the negative weight change is maximum. This is described graphically in Figure VI-7b and can be written mathematically as:

$$c(t) = \int \left( \delta(t - t_{post}) - \alpha * c(t) \right) dt$$
$$c'(t) = u(t - t_{post}) - c(t)$$

$$dwn = L_{RateN} * \left( \delta(t - t_{pre}) * c'(t) + pre \ doesnt \ spike * \delta(t - t_{post}) \right)$$
$$= L_{RateN} * c'(t_{pre})$$

Where dwn is the negative weight change and  $L_{RateN}$  is the negative learning rate.

### 6.4.2 Challenge 2: Inhibition

As I argued in chapter 5, Winners-Share-All algorithm requires only half of the neurons at the output to fire. In order to enforce this requirement, we need to ensure that:

- a) No neuron fires more than once in a specific time window.
- b) With 6 output neurons, upon the arrival of the third spike, all other neurons need to be inhibited.

Figure VI-8 shows the solutions employed to establish the above conditions. A selfinhibitory connection at each output neuron ensures that no neuron spikes more than once in any given time window since the neuron undergoes an inhibition upon spiking (condition a). The inhibitory neuron in Figure VI-8 accumulates the spikes emitted from the pool of the output neurons and its threshold is set so that it fires after the third spike has been generated hence inhibiting all the neurons at the output (condition b). We can model the inhibitory neuron with the following mathematical expression:

$$V_{mem_{inhibit}}(t) = \int_{(n-1)T}^{t} \left( Spikes_{layer3} - \alpha_{inhib} * V_{mem-inhibit}(t) \right) dt$$

$$(n-1)T < t < nT$$

$$Inhibit = \begin{cases} 1 & V_{mem} > V_{th-inhibit} \\ 0 & Otherwise \end{cases}$$

$$V_{mem-inhibit}(nT) = 0$$

$$n = 0, 1, 2, \dots, floor\left(\frac{t}{t_{end}}\right)$$

And therefore each output neuron i can be described as:

$$V_{mem_{out}}^{i}(t) = \int_{(n-1)T}^{t} (Spikes_{layer2} - \alpha_{leak} * V_{mem_{out}}^{i}(t) - Inhibit - \delta(t - t_{spike^{i}})) dt$$
$$(n-1)T < t < nT$$

Where  $V_{mem_{out}}^{i}$  refers to the i<sup>th</sup> output neuron membrane potential and  $\delta(t - t_{spike^{i}})$  is the spike emitted from the same output neuron which represents self-inhibition employed to ensure the neuron does not spike more than once in any given time window.



Figure VI-8 Inhibitory neuron designed to ensure not more than half of the output neurons fire at any given time window.

### 6.4.3 Challenge 3: Correlation in the input patterns

In this problem we have a set of synthetic and relatively small images which results in high correlation between pixels. Hence, there is similarities between the patterns which makes it more likely for different patterns to be recognized as a single one and therefore it's challenging to separate them as different classes. The solution I employed for this problem is what I call *habituation* because it diminishes the innate response of the neurons to a frequently repeated stimulus. In habituation, the network finds the similarities between the patterns and ignore



Figure VI-9 Habituation neuron designed to ignore the similarities between the input patterns and look for the differences between patterns which helps to separate patterns.

them and instead looks for dissimilarities. This is illustrated in Figure VI-9. An intermediate *habituation* leaky integrate and fire neuron is introduced between each neuron in layer 2 and layer 3. It receives its input from the neuron in layer 2 and its output spikes modifies the connection between the corresponding neurons in layer 2 and layer 3. The threshold of this habituation neuron is set so that it can detect the frequent firing of its input neuron in layer 2. The frequent firing of such neuron identifies a common feature in that specific location on the image. Information theoretically, that feature contains very little information about the pattern since it's very *probable* to happen and therefore has a low entropy and can be ignored. The habituation neuron can be defined as:

$$V_{mem,habit}(t) = \int_{0}^{t} (Spikes_{layer2} - \alpha_{hab} * V_{mem,habit}) dt$$
$$habit = \begin{cases} 1 & V_{mem_{habit}} > V_{th_{habit}} \\ 0 & Otherwise \end{cases}$$

Note that unlike other neurons that we have so far introduced, the habituation neuron does not reset at the end of the time window since it has to keep the history of the patterns. It only resets when it reaches the threshold and fires a spike. The modification of weight due to habituation is modeled below:

$$dw_{i,j} = \alpha \left( dwp_{i,j} - dwn_{i,j} \right) - \beta * \delta(t - t_{habit i,j}) * exp(-\gamma t)$$

where dwp<sub>ij</sub> and dwn<sub>ij</sub> are the positive and negative changes of weight due to STDP between neurons i,j in layer 2 and 3 which I explained in section 6.4.2.  $\delta(t - t_{habit i,j})$  are the spikes from the habituation neuron which are decreasing the weight between neurons i and j as discussed above. However, there is an exponential decay associated with the habituation since as the network learns the input data the effect of it should become less and less in order to encourage convergence. This works similar to the heuristics generally applied to learning rate in neural network in order to achieve convergence faster.

#### 6.4.4 Challenge 4: Greedy Attractor

#### a) Homeostatic Plasticity

Neuronal activity is the key to learning by the changes of synaptic connectivity through the 'Hebbian' mechanism or in the spike form, 'Spike Timing Dependent Plasticity (STDP)'. However, STDP is a non-controlled growth or decay of synaptic 'weights' and hence, a destabilizing force in neural circuits. For example, in the context of WSA algorithm, if one combination starts off being favorable for multiple patterns, hebbian based learning will encourage that behavior (since it's a positive feedback mechanism) and the weights run off to the extremes and hence lose a lot of information.



Figure VI-10 Concept of homeostatic plasticity in the brain. Feedback mechanisms are applied in order to keep the firing rate of a neuron in a target range. Figures are taken from [32].

One proposed idea to solve this problem is that the average neuronal activity is maintained within a range by homeostatic plasticity mechanism which dynamically adjust synaptic strength in the correct direction to promote stability [32].

The authors in [32] argue that the data from *in vitro* cortical networks indicate that homeostatic synaptic plasticity rules independently adjust excitatory and inhibitory feedback loops within recurrent cortical networks so that activity is preserved despite change in drive. When activity falls too low (because, for example, sensory drive is reduced), excitation between pyramidal neurons is boosted and feedback inhibition is reduced (Figure VI-10). This should raise the firing rates of pyramidal neurons. Conversely, when activity is too high, excitation between pyramidal neurons is reduced, and excitation onto interneurons and inhibitory inputs back onto pyramidal neurons are increased, thereby boosting feedback inhibition. This should lower the activity of pyramidal neurons. So, homeostatic regulation of network activity in recurrent cortical circuits is accomplished through a coordinated set of changes that selectively adjust different classes of synapse to drive network activity towards some set point. Employing homeostatic property has two main advantages:

- It will not let one output neuron (or in our case one combination) get very greedy and respond to many input patterns. In other words, it will "watch" the competition and make sure all the combinations will get a chance to respond to some input pattern.
- 2) It will also act as a *regularizer* for the neural network to avoid overfitting. Overfitting is a concept in machine learning where the network starts fitting too well to the training set and loses generalization and hence do not do well on the testing set. In this case network parameters start changing because of the "noise" in the data set and have a poor performance in recognizing patterns that have not been presented to it before. Regularization will make sure to control the growth of the weights in a way that the network response to small random variations in the input is minimal which is also what the homeostatic property is doing.

#### b) Homeostatic Plasticity in action

To dynamically adjust synaptic strength in the correct direction to promote stability in the weights, we need to first identify the greedy behavior in neurons. Therefore, we need a type of "Neural State Machine (NSM)" to recognize if a neural state is happening *too often* or *too rarely*. Figure VI-11 illustrates this idea. Each neuron in the state machine is assigned to respond to the advent of a certain combination or state. Since we have enforced the condition of a maximum number of 3 (half of the output neurons) to fire at every time bin, then every neuron in the state machine takes input from 3 neurons which make a unique combination. The leaky integrator and fire neuron is designed to fire after detecting the 3 neuron firing at its input. As a result of that at each time window, the spikes out of the neural state machine



Figure VI-11 Neural State Machine (NSM) designed to control the appearance frequency of the WSA codes. indicate the combination that has occurred. The inset in Figure VI-11 depicts the detection of the combination 1,2,3 from the first neuron in the NSM.

Now, to find out if a combination is happening too often or too rare and correct it, we feed the spikes from the neural state machine with detected combinations to a block with leaky integrator units. The time constant of these leaky integrators are a design choice and has to be picked in order to determine what it means to be *too often* or *too rare* depending on the network behavior. Each leaky integrator (LI) parameter keeps the history of every combination occurrence and if it's greater than a certain threshold of  $V_{th,p}$  it generates a spike which translates to that combination being happening *too often*. On the contrary, if the LI parameter goes below a threshold of  $V_{th,n}$ , a spike will be generated which means that the combination is dormant and is taking place *too rare*.

This can be mathematically described as below:

$$V_{mem_{NSM}}^{i}(t) = \int_{(n-1)T}^{t} \left(\sum_{j=k1^{i}}^{k3^{i}} \delta\left(t - t_{spike,j}\right) - \alpha_{3} * V_{mem_{NSM}}^{i}(t)\right) dt$$
$$(n-1)T < t < nT$$

 $k1^i, k2^i, k3^i \in \{\text{neurons in the i}^{\text{th}} \text{combination}\}$ 

$$Spike_{NSM}^{i} = \begin{cases} 1 & V_{mem_{NSM}}^{i} > V_{th,NSM} \\ 0 & Otherwise \end{cases}$$
$$LIComb^{i}(t) = \int_{0}^{t} (Spike_{NSM}^{i} - \alpha_{2} * CombFreqDet^{i}) dt$$
$$CombFreqDet^{i}(t) = LIComb^{i}(t) + \xi$$

Where  $\xi$  is a positive bias added to the output of the integrator as a DC shift in order to detect the non-spiking combination through the decay parameter going below the low threshold:

$$CombTooOFten = \begin{cases} 1 & CombFreqDet > V_{th,p} \\ 0 & Otherwise \end{cases}$$
$$CombTooRare = \begin{cases} 1 & CombFreqDet < V_{th,n} \\ 0 & Otherwise \end{cases}$$

We can now use the information from the combination occurrence frequency in order to correct the direction of network convergence to promote stability. One way of doing so which is inspired by the work in [33] is to use each "too often spikes (TOS)" to increase the threshold of the neurons in the combination and to use each "too rare spike (TRS)" to decrease the threshold of the corresponding neurons. Increasing the threshold decreases the activity of the neurons and decreasing it increases their activity so it will put the system in a negative feedback loop which controls the combination frequency within a range as was discussed in the part a of this section (Figure VI-11). The OR gates in the figure are used to shrink the outputs from

the number of combinations to the number of output neurons. j<sup>th</sup> OR at the top is summing the TOS including neuron j and i<sup>th</sup> OR at the bottom is doing so for TRS including neuron i.

However, since we were dealing with combinations of neuron firing here, a neuron might be contributing in TOS at the same time as it is doing so for TRS. To make that clear let me give an example. If combination "1,2,3" is happening too often and "1,4,6" is not being seen at all, then neuron 1's threshold should increase because of the TOS and also decrease because of TRS. Therefore, we need an averaging mechanism to determine how the threshold of each neuron has to change *on average*. That can be achieved by using another set of integrators which keep track of the history of TOS and TRSs. This is illustrated graphically in Figure VI-11. The output of these averaging neurons are used to modify the threshold of the output neurons with a feedback shown in green in the Figure.

$$\begin{aligned} Averager_{P}^{i}(t) &= \int_{0}^{t} (\sum_{j} (CombTooOften^{j}) - \alpha_{3} * Averager_{P}^{i}(t)) dt \\ Averager_{N}^{i}(t) &= \int_{0}^{t} (\sum_{j} (CombTooRare^{j}) - \alpha_{3} * Averager_{N}^{i}(t)) dt \\ j &\in \{all \ combinations \ inluding \ the \ i^{th} neuron\} \\ V_{th}^{i}(t) &= V_{th0} - \beta_{1} * Averager_{P}^{i}(t) + \beta_{2} * Averager_{N}^{i}(t) \end{aligned}$$

# 6.5 Results

### 6.5.1 Weight Evolution

Weights of the output neurons are initialized using normal distributed random numbers. The mean is chosen to be small since we have noticed by choosing large means closer to 1, the weights get saturated very fast and learning stops. The standard deviation of the normal distribution has to be chosen large enough to separate the weights sufficiently in the beginning but also not so large that the weights saturate. After 140 epochs of training, looking at the weight evolution of the connections to layer 3 as is shown in Figure VI-12, it's apparent that they take analog values between zero and one. The weights don't run off to the maximum and minimum and maintained in the analog region by the negative feedback mechanisms employed in the network. These analog weights provide us with a lot more information capacity to encode



Figure VI-12 Weight evolution showing the weights converging to analog values.

the input scene.



Figure VI-13 Spikes from the output neurons. Zoomed in view is showing that half of the neurons don't necessarily spike at each clock cycle.

### 6.5.2 Output Neurons Output

Let us now look at the output of the network as is depicted in Figure VI-13. In each time window of 10 ms, the outputs of 6 output neurons are monitored and are shown as raster plots. But as can be noticed, not all the 3 output neurons fire at all times since we only ensured that not more than 3 neurons fire, but we never enforced exactly 3 neurons to fire. Moreover, it seems rather unnatural to force exactly half of the neurons to fire in response to every pattern and looking at it more carefully, this can potentially increase the code space even more. This way, in the code space, not only we have combinations of 3 out of 6 neurons firing, but also we can have combinations of every pair of neurons, and also only one neuron to fire in response to patterns. This increases the code space for 6 output neurons to:

$$\binom{6}{3} + \binom{6}{2} + \binom{6}{1} = 41$$

And in a more generalized form for n output neurons to:

Code Space Size = 
$$\sum_{k=1}^{\frac{n}{2}} {n \choose k}$$

### 6.5.3 Classification

The ultimate measure of how well Winners-Share-All algorithm works is by determining the classification accuracy on the test set which the network was not presented by during training. This is shown in Figure VI-14. The network performance on the test set reaches 87%. Note that since this is a small synthetic image set, the separation of the patterns is more difficult than natural images. In the figure it's also shown how different patterns from Figure VI-1, numbered orderly from 1 to 14, are assigned to unique combinations from the code space and hence are separate by the network.

This codes are highlighted in Figure VI-14 by black circles which are picked by the maximum number of counts for a code per pattern.



Figure VI-14 Network performance on the test set. On the left, the network accuracy converges to 87%. On the right, each pattern gets assigned to a unique combination from a set of 41 codes in the code space.


Figure VI-15 Edit distance vs Pattern similarity for all the patterns.

#### 6.5.4 Discussion

The network starts with a random initial condition and over the course of training picks certain codes for each pattern. One interesting study is to see if there is any correlation between the "distance" of the patterns and the "distance" of the codes that are being picked. The former can be measured by the similarity between the patterns which I'm defining as the number of common pixels between the patterns while the former is simply the edit distance between the codes. Edit distance is a way of quantifying how dissimilar two strings are to one another by counting the minimum number of operations needed to transform one string to the other. For example, the edit distance between two codes of '1,2,3' and '3,4,5' are 2, since 2 substations are needed to transform one to the other. For each pattern I plot the edit distance of the code assigned to it during the simulation versus its similarity to all other patterns. This is shown in Figure VI-15. The data points are the average of data for 3 initial condition. As can be seen from the figure, the probability of lower edit distance goes higher as the similarity between the patterns increases. This can be confirmed in the case where all the pixels are the same (self-comparison), the code is the same and hence the edit distance is zero. Therefore, the output of the network, gives us another piece of information other than the recognition, and that is how similar the patterns are.

#### VII. Conclusion and Future Work

#### 7.1 Conclusion

In this thesis I address the issues that the neuromorphic field faces in terms of number of connections needed on chip to perform brain-like functions. I explain the two-pronged method I investigated in order to tackle this problem.

Firstly, the advent of memristors as nano-size devices which can be 3D integrated on top of CMOS chips guided us through making platforms in the CMOS process to utilize them as possible memory devices and also as synaptic connections between the CMOS neurons. Two chips were taped out to explore these possibilities. First chip was realized as a configurable memory platform designed with the CMOL architecture providing appropriate programming and sensing circuitry along with the decoding to access the memory cells. This chip was successfully used by our collaborators for 3D integration and its configurability enabled the required supporting circuitry for different types of memristors. Second chip was also designed as a configurable pool of CMOS neurons designed under the CMOL architecture. The CMOS neurons generate programmable pulse shapes which are engineered to implement online learning through STDP while driving the memristive crossbar array.

Secondly, by taking advantage of the coding theory, I was able to develop a novel algorithm to exploit the coding space provided by the spiking neural networks. I introduced the concept of Winners-Share-All as a replacement for Winner-Takes-All which takes a combinatorial approach in coding the spikes emitted from the output neurons. By employing this algorithm less number of neuronal agent is required to perform classification tasks and hence it also reduces the number of connections and training parameters. In the thesis, I point out the



Figure VII-1 400 features extracted from MNIST training set by training an autoencoder.

challenges encountered by using this algorithm and how I used a network of recurrent neurons to overcome them. I used this algorithm to classify 14 artificial images using only 6 output neurons and achieved a classification accuracy of 87% using a completely unsupervised approach.

#### 7.2 Future Directions

I used the Winners-Share-All algorithm to classify artificial images. In order to show the true power of this algorithm, it has to be tested against standard platforms such as the handwritten digit data set known as MNIST. Similar approaches utilized for the artificially made data set can be taken for MNIST. Firstly, the features of MNIST images need to be extracted in the form of filters to be used in a Convolutional Neural Network. This can be done by training an auto-encoder which is being applied on randomly chosen patches of the MNIST training data set. The patches need to have the same size as we desire for the filters. The auto-encoder finds the basis vectors by which the images in the dataset can be defined. Figure VII-1shows the features extracted from MNIST by training an auto-encoder with a hidden size

of 400 and a visible size of 7x7 which is the size of the patches randomly chosen from MNIST training set. These filters can then be used to extract the features of every single image in the training data set which will be transformed in the form of spikes. The last layer of the network will be identical to the one we used in this thesis.

This coding algorithm could also be expanded to work at every layer. In other words, all the layers of a deep network can be coded using this algorithm. Doing so will be extremely efficient in terms of area since the exploitation of the temporal code is being utilized at every layer and the number of parameters will reduce at each layer by the  $\alpha$  parameter of WSA.

## References

- D. Modha, "Introducing a Brain-inspired Computer." [Online]. Available: http://www.research.ibm.com/articles/brain-chip.shtml.
- B. Linares-Barranco and T. Serrano-Gotarredona, "On the design and characterization of femtoampere current-mode circuits," *IEEE J. Solid-State Circuits*, vol. 38, no. 8, pp. 1353–1363, 2003.
- [3] S. Mitra, S. Fusi, and G. Indiveri, "Real-time classification of complex patterns using spike-based learning in neuromorphic VLSI," *IEEE Trans. Biomed. Circuits Syst.*, vol. 3, no. 1, pp. 32–42, 2009.
- [4] T. Pfeil, T. C. Potjans, S. Schrader, J. Schemmel, M. Diesmann, and K. Meier, "Is a 4-bit synaptic weight resolution enough? constraints on enabling spike-timing dependent plasticity in neuromorphic hardware," *Front. Neurosci.*, no. JULY, pp. 1–19, 2012.
- [5] C. Diorio, P. Hasler, A. Minch, and C. a. Mead, "A single-transistor silicon synapse," *IEEE Trans. Electron Devices*, vol. 43, no. 11, pp. 1972–1980, 1996.
- [6] R. Serrano-Gotarredona, T. Serrano-Gotarredona, A. Acosta-Jiménez, and B. Linares-Barranco, "A neuromorphic cortical-layer microchip for spike-based event processing vision systems," *IEEE Trans. Circuits Syst. I Regul. Pap.*, vol. 53, no. 12, pp. 2548– 2566, 2006.
- [7] K. K. Likharev and D. B. Strukov, "CMOL: Devices, Circuits, and Architectures."
- [8] W. Lu, K. H. Kim, T. Chang, and S. Gaba, "Two-terminal resistive switches (memristors) for memory and logic applications," *Proc. Asia South Pacific Des.*

Autom. Conf. ASP-DAC, pp. 217–223, 2011.

- [9] J. J. Yang, D. B. Strukov, and D. R. Stewart, "Memristive devices for computing.," *Nat. Nanotechnol.*, vol. 8, no. 1, pp. 13–24, 2013.
- [10] A. Ghofrani, M. A. Lastras-Montano, and K. T. Cheng, "Towards data reliable crossbar-based memristive memories," *Proc. - Int. Test Conf.*, 2013.
- [11] M. S. Qureshi, M. Pickett, F. Miao, and J. P. Strachan, "CMOS interface circuits for reading and writing memristor crossbar array," *Proc. IEEE Int. Symp. Circuits Syst.*, pp. 2954–2957, 2011.
- [12] D. B. Strukov and K. K. Likharev, "CMOL FPGA: a reconfigurable architecture for hybrid digital circuits with two-terminal nanodevices," *Nanotechnology*, vol. 16, no. 6, pp. 888–900, 2005.
- [13] M. A. Lastras-Montano, A. Ghofrani, and K. T. Cheng, "Architecting energy efficient crossbar-based memristive random-access memories," *Proc. 2015 IEEE/ACM Int. Symp. Nanoscale Archit. NANOARCH 2015*, no. 2, pp. 1–6, 2015.
- [14] J. Rofeh, A. Sodhi, M. Payvand, M. A. Lastras-monaño, A. Ghofrani, A. Madhavan,
   S. Yemenicioglu, K. Cheng, and L. Theogarajan, "Vertical Integration of Memristors onto Foundry CMOS Dies using Wafer-Scale Integration," pp. 1–5.
- [15] M. Payvand, A. Madhavan, M. A. Lastras-montaño, A. Ghofrani, J. Rofeh, D. Strukov, and L. Theogarajan, "A Configurable CMOS Memory Platform for 3D-Integrated Memristors."
- [16] G. Q. Bi and M. M. Poo, "Synaptic modifications in cultured hippocampal neurons: dependence on spike timing, synaptic strength, and postsynaptic cell type.," *J. Neurosci.*, vol. 18, no. 24, pp. 10464–10472, 1998.

- [17] T. Chang, S. H. Jo, K. H. Kim, P. Sheridan, S. Gaba, and W. Lu, "Synaptic behaviors and modeling of a metal oxide memristive device," *Appl. Phys. A Mater. Sci. Process.*, vol. 102, no. 4, pp. 857–863, 2011.
- [18] C. Zamarreño-Ramos, L. a. Camuñas-Mesa, J. a. Perez-Carrasco, T. Masquelier, T. Serrano-Gotarredona, and B. Linares-Barranco, "On spike-timing-dependent-plasticity, memristive devices, and building a self-learning visual cortex," *Front. Neurosci.*, vol. 5, no. MAR, pp. 1–22, 2011.
- [19] M. Prezioso, F. Merrikh Bayat, B. Hoskins, K. Likharev, and D. Strukov, "Self-Adaptive Spike-Time-Dependent Plasticity of Metal-Oxide Memristors," *Sci. Rep.*, vol. 6, no. February, p. 21331, 2016.
- [20] M. Prezioso, F. Merrikh-Bayat, B. D. Hoskins, G. C. Adam, K. K. Likharev, and D. B. Strukov, "Training and operation of an integrated neuromorphic network based on metal-oxide memristors.," *Nature*, vol. 521, no. 7550, pp. 61–4, 2015.
- [21] L. Wang and L. Theogarajan, "A micropower delta-sigma modulator based on a self-biased super inverter for neural recording systems," *Proc. Cust. Integr. Circuits Conf.*, 2010.
- [22] O. Bichler, D. Querlioz, S. J. Thorpe, J. P. Bourgoin, and C. Gamrat, "Extraction of temporally correlated features from dynamic vision sensors with spike-timingdependent plasticity," *Neural Networks*, vol. 32, pp. 339–348, 2012.
- [23] M. D. Pardoen and M. G. Degrauwe, "Rail-to-rail input/output CMOS power amplifier," *IEEE J. Solid-State Circuits*, vol. 25, no. 2, pp. 501–504, 1990.
- [24] W. S. McCulloch AND W. Pitts, "A Logical Calculus of the ideas Immanent in Nervous Activity," *Bull. Math. Biophys.*, vol. 5, pp. 115–133, 1943.

- [25] S. Thorpe, A. Delorme, and R. Van Rullen, "Spike-based strategies for rapid processing," *Neural Networks*, vol. 14, no. 6–7, pp. 715–725, 2001.
- [26] F. Ahmed, B. Yusob, and H. Hamed, "Computing with Spiking Neuron Networks: A Review," Int. J. Adv. Soft Comput. Appl., vol. 6, no. 1, pp. 1–21, 2014.
- [27] C. E. Shannon, "A Mathematical Theory of Communication," *Bell Syst. Tech. J.*, vol. 27, pp. 379–423, 1948.
- [28] A. Coates and A. Ng, "Selecting Receptive Fields in Deep Networks.," *Nips*, no. i, pp. 1–9, 2011.
- [29] P. Dayan and L. F. Abbott, "Theoretical Neuroscience: Computational and Mathematical Modeling of Neural Systems," *Comput. Math. Model. Neural* ..., p. 480, 2001.
- [30] R. Guyonneau, R. VanRullen, and S. J. Thorpe, "Temporal codes and sparse representations: A key to understanding rapid processing in the visual system," *J. Physiol. Paris*, vol. 98, no. 4–6 SPEC. ISS., pp. 487–497, 2004.
- [31] "Convolutional Neural Network." [Online]. Available: http://ufldl.stanford.edu/tutorial/supervised/ConvolutionalNeuralNetwork/.
- [32] A. Maffei, D. Bucher, and A. Fontanini, "Homeostatic plasticity in the nervous system," *Neural Plast.*, vol. 2012, 2012.
- [33] P. Sheridan, W. Ma, and W. Lu, "Pattern Recognition with Memristor Networks," *IEEE Int. Symp. Circuits Syst.*, pp. 1078–1081, 2014.
- [34] C. Mead, *Analog VLSI and Neural Systems*. Addison Wesley Publishing Company, 1989.
- [35] P. Hasler, C. Diorio, B. A. Minch, and C. Mead, "Single transistor learning synapses,"

in Advances in Neural Information Processing Systems 7, 1995, pp. 817–824.

- [36] J. E. Smith, "Biologically Plausible Spiking Neural Networks," pp. 1–82, 2015.
- [37] L. Vanneschi and E. Systems, *Handbook of Natural Computing*. 2012.

## Appendix I: MATLAB Code developed for Layer 1: Image

# Intensity to Spike Conversion

```
%Multi Neuron first layer----mROC all excitatory
% initialize parameters
Sthe size of Y should at least be the simulation end time divided by 10
dt = 0.5;
%nSide=size(H,1);
nSide=15;
n lstLayer=nSide*nSide;
nint=0;
% reserve memory
T = ceil (92400/dt) ; %The number should be maximum 10*the size of the Y
vth1= 55;
v = zeros (n 1stLayer,T) ; % n x T, v: membrane potential
v (:,1) =0; % vectors
Iapp= 1000* Y;
% for loop over time
for t =1:T-1;
    if floor(t*0.5/10) == t*0.5/10
        tint=t;
        nint=floor(t*0.5/10);
        v(:, t) = 0;
    end
    Input=Iapp(:,nint+1)*dt; %sampling Y at the beginning of the frame
rate clock and keeping it up until the next sample
    %update vectorized ODE
    v(:,t+1) = v(:,t)+Input ;
    %handle spikes ( reset v )
    fired = v(:,t)>= vth1; % neurons fired? find the ones whose membrane
potential is greater than vth
    v(fired ,t) = vth1;
    v(fired , t+1) = 0;
    Iapp(fired, nint+1) =0;
end
%plot spike raster
spks = double(v==vth1);
clf , hold on ;
[X,Y3] = meshgrid((0:T-1)*dt,1:n 1stLayer) ;
```

```
idx = find(spks==1) ;
plot (X(idx),Y3(idx) ,['r','.'] ) ; %inhibitory: k=2, plot is red.
Excitatory: k=1, plot is black
xlim([0,T*dt]);
%xlim([0,100]);
ylim([0,n_1stLayer]);
xlabel('Time[ms]')
ylabel('Unit #')
```

## Appendix II: MATLAB Code developed for Layer 2:

## **Extracting Features**

```
%Generating the kernels
KernelSize=3;
Kernel 45=zeros(KernelSize,KernelSize);
Kernel_135=zeros(KernelSize,KernelSize);
Kernel Vert=zeros(KernelSize,KernelSize);
Kernel Horz=zeros (KernelSize, KernelSize);
for i=1:KernelSize
    for j=1:KernelSize
        if i==j
         Kernel 135(i,j)=1;
        else
            Kernel 135(i,j)=-0.5;
        end
        if i+j==KernelSize+1
            Kernel 45(i,j)=1;
        else
            Kernel_45(i,j)=-0.5;
        end
        if i==(1+KernelSize)/2
            Kernel Horz(i,:)=1;
        else
            Kernel_Horz(i,:)=-0.5;
        end
        if j==(1+KernelSize)/2
            Kernel Vert(:,j)=1;
        else
            Kernel Vert(:,j)=-0.5;
        end
    end
end
%Multi Neuron Edge Detection Layer----mROC all excitatory
% initialize parameters
dt = 0.5;
ImageSide=15;
n 2ndLayer=4*(ImageSide/KernelSize)*(ImageSide/KernelSize);
nint=0;
TFR=10;
inhibit=zeros(n 2ndLayer,1);
inhibit others=0;
% reserve memory
T = ceil (92400/dt);
```

```
vth2= 3;
v2 = zeros (n 2ndLayer,T) ; % n x T, v: membrane potential
v2(:,1) =0;
              % vectors
Input2=zeros(225,T);
Y 45Deg=zeros(9,1); % one number for each edge at every kernel
Y 135Deg=zeros(9,1);
Y Horz=zeros(9,1);
Y Vert=zeros(9,1);
Edge=zeros(100,1);
%Edge Detection Kernels
Kernel 45Deg=reshape(Kernel 45, [1 9]);
Kernel Vert=reshape(transpose(Kernel Vert), [1 9]);
Kernel 135Deg=reshape(Kernel 135, [1 9]);
Kernel Horz=reshape(transpose(Kernel Horz), [1 9]);
% for loop over time
for t =1:T-1;
    % Reseting values at the frame rate clock cycle
    if floor(t*dt/TFR) ==t*dt/TFR
        tint=t;
        nint=floor(t*dt/TFR);
       v2(:,t)=0;
                            % reset membrane potential
        Input2(:,t)=0;
                            % Reset the input
                            % Reset inhibit signal
       inhibit=0;
       inhibit others=0;
    end
    Input2(:,t+1)=Input2(:,t)+spks(:,t+1); %If there is an spike in the
time frame, keep it until the end of the time window.
    %applying kernels to the input's window
    for i=1:1:25
        Y 45Deg(i,1) = Kernel 45Deg* Input2(9*i-8:9*i,t);
        Y 135Deg(i,1) = Kernel 135Deg* Input2(9*i-8:9*i,t);
        Y Horz(i,1) = Kernel Horz* Input2(9*i-8:9*i,t);
        Y Vert(i,1) = Kernel Vert*Input2(9*i-8:9*i,t);
        Edge(i*4-3:i*4,1)=[Y 45Deg(i);Y Vert(i);Y 135Deg(i);Y Horz(i)];
    end
    %Input1(:,nint+1)=Iapp(:,nint+1)*dt;
    %update vectorized ODE
    v2(:,t+1) = v2(:,t)+ (Edge)*dt-inhibit(:,1)-0.2*inhibit others;
    %handle spikes ( reset v )
    inhibit=zeros(n 2ndLayer,1);
    fired2 = v2(:,t)>= vth2; % neurons fired? find the ones whose
membrane potential is greater than vth
```

```
v2(fired2 ,t) = vth2;
v2(fired2 ,t+1) = 0;
inhibit(fired2)=20;
inhibit_others=sum(fired2);
%Input2(fired2,t+1) =0;
```

#### end

```
%plot spike raster
spks2 = double(v2==vth2);
clf , hold on ;
[X_2,Y3_2] = meshgrid((0:T-1)*dt,1:n_2ndLayer) ;
```

```
idx_2 = find(spks2==1) ;
plot (X_2(idx_2),Y3_2(idx_2) ,['r','.'] ) ;
```

```
xlim([0,T*dt]);
%xlim([0,100]);
ylim([0,n_2ndLayer]);
xlabel('Time[ms]')
ylabel('Unit #')
```

#### %normalizing the spikes

```
T1=size(spks2,2);
sum_period=zeros(1,T1);
DIVIDE_SUM=zeros(1,T1);
spks2 normalized=zeros(size(spks2));
```

```
for t =1:T1;
    if t==1
        sum_period(t)=0;
    else
        sum_period(t)=sum(spks2(:,t))+sum_period(t-1);
    end
    if floor(t*dt/TFR)==t*dt/TFR
        DIVIDE_SUM(t-19:t)=sum_period(t-1);
        sum_period(t)=0;
    end
end
for t=1:T1-1
    spks2 normalized(:,t)=spks2(:,t)./DIVIDE_SUM(:,t);
```

```
end
```

# Appendix III: MATLAB Code Developed for Layer 3:

### Classification

```
%third layer for classification
% initialize parameters
clc
dt = 0.5;
n 2ndLayer=100;
n 3rdLayer=6;
nint=0;
TFR=10;
inhibit weak=zeros(n 3rdLayer,1);
k n3tau=0.5;
            %neuron time constant%
IC=normrnd(0.04,0.12,[n 2ndLayer*n 3rdLayer 1]); %Initial condition
vth3 nominal=ones(6,1)*0.35;
vth comb=3;
vth comb1=1;
vth homeo pos1=2.8;
vth homeo neg1=0.3;
vth_homeo_pos3=1.8;
vth homeo neg3=0.25;
k3=0.006; %Threshold change time constant
k3 ex=0.003;
k3 single=0.001; %Threshold change time constant
k3 ex single=0.006;
alpha hab=0.01;
vth hab=3;
kCTRL=0.04;
vth CTRL neg=2;
vth CTRL pos=0.4;
k homeo=0.01;
%STDP PARAMS------
alpha=0.1; %STDP time constant. The sooner it dies, the sooner the
effect of a (Pre, Post) spike goes away
LRateN=0.0001; %Negative learning rate
NumofInput=n 2ndLayer; %Number of inputs from the edge detection layer
NumofOutput=n 3rdLayer; %Number of output neurons in the classification
layer
```

```
% reserve memory -----
T = ceil (80000/dt);
v3 = zeros(n 3rdLayer,T); % n x T, v3: membrane potential
v3(:,1) =0;
             % vectors
Pre PWM singleNeuron=zeros(n 2ndLayer,T);
Pre PWM SN norm=zeros(n 2ndLayer,T);
INN=zeros(n 2ndLayer,1);
posts=zeros(n 2ndLayer*n 3rdLayer,T);
LInt1=zeros(n 2ndLayer*n 3rdLayer,T);
LInt2=zeros(n_2ndLayer*n_3rdLayer,T);
Input3_weighted=zeros(n 3rdLayer,1);
CombDtct1=zeros(6,T);
CombDtct2=zeros(15,T);
CombDtct=zeros(20,T);
Spike_Comb_time=zeros(20,T);
OUT1 homeo=zeros(6,T);
OUT3 homeo=zeros(20,T);
OUTPUT homeol=zeros(6,T);
OUTPUT homeo3=zeros(20,T);
homeo pos spike=ones(20,T);
homeo neg spike=ones(20,T);
homeo pos spike1=ones(6,T);
homeo neg spikel=ones(6,T);
Exc1 OUT=zeros(n 3rdLayer,T);
Inh1 OUT=zeros(n 3rdLayer,T);
Exc OUT=zeros(n 3rdLayer,T);
Inh OUT=zeros(n_3rdLayer,T);
spike inhib=zeros(n 3rdLayer,T);
spike exc=zeros(n 3rdLayer,T);
habituation=zeros(size(spks2,1),T);
habituation all=zeros(size(spks2,1)*6,T);
FR CTRL=zeros(6,T);
FR1=zeros(6,T);
posts CTRL=zeros(6,T);
check fire=zeros(6,T);
CTRL UP vth=zeros(6,T);
CTRL DN vth=zeros(6,T);
MAX Indx=zeros(6,1);
NumberFired=zeros(1,T);
%STDP matrices -----
```

```
Pre=zeros(n 2ndLayer*n 3rdLayer,T);
Pre PWM=zeros(n 2ndLayer*n 3rdLayer,T);
Pre PWM norm=zeros(n 2ndLayer*n 3rdLayer,T);
Post_PWM=zeros(n_2ndLayer*n_3rdLayer,T);
dwP=zeros(NumofInput*NumofOutput,T);
dwN=zeros(NumofInput*NumofOutput,T);
dw=zeros(NumofInput*NumofOutput,T);
w=zeros(NumofInput*NumofOutput,T);
y1 STDP=zeros(NumofInput*NumofOutput,T);
y2 STDP=zeros(NumofInput*NumofOutput,T);
tint=20;
vth time=zeros(6,T);
vth3=vth3 nominal;
% for loop over time-----
for t =1:T-1;
    %LRateN=0.0002*exp(-0.000025*t); %Negative learning rate
    LRateP=0.0072*exp(-0.00003*t); %Positive learning rate
    % Reseting values at the frame rate clock cycle
    if floor(t*dt/TFR) == t*dt/TFR
        tint=t;
        nint=floor(t*dt/TFR);
        v3(:,t)=0;
                            % reset membrane potential
        Pre PWM singleNeuron(:,t)=0; % Reset the input
        Pre PWM SN norm(:,t)=0;
        inhibit strong=0;
                                  % Reset inhibit signal
        inhibit weak=0;
       Pre PWM(:,t)=0;
                            % Reset the SR latch with the Pre connected
to it
       Post PWM(:,t)=0;
                            % Reset the SR latch with the Post connected
to it
       Pre PWM norm(:,t)=0;
        y1 STDP(:,t)=0;
        y2 STDP(:,t)=0;
       LInt1(:,t)=0;
        LInt2(:,t)=0;
        dwP(:, t) = 0;
        dwN(:, t) = 0;
        CombDtct(:,t)=0;
        CombDtct2(:,t)=0;
       NumberFired(t-1)=0;
       MAX Indx=zeros(6,1);
    end
    w(:, 1) = IC;
    Pre PWM singleNeuron(:,t+1)=Pre PWM singleNeuron(:,t)+spks2(:,t+1);
%If there is an spike in the time frame, keep it until the end of the time
window.
Pre PWM(:,t)=[Pre PWM singleNeuron(:,t);Pre PWM singleNeuron(:,t);Pre PWM
singleNeuron(:,t);Pre PWM singleNeuron(:,t);Pre PWM singleNeuron(:,t);Pre
PWM singleNeuron(:,t)]; %NEW
Pre(:,t)=[spks2(:,t);spks2(:,t);spks2(:,t);spks2(:,t);spks2(:,t);spks2(:,t)
)];
```

```
103
```

```
Pre PWM SN norm(:,t+1)=Pre PWM SN norm(:,t)+spks2 normalized(:,t+1);
Pre PWM norm(:,t)=[Pre PWM SN norm(:,t);Pre PWM SN norm(:,t);Pre PWM SN no
rm(:,t);Pre PWM SN norm(:,t);Pre PWM SN norm(:,t);Pre PWM SN norm(:,t)];
   if t==1
       habituation(:,t)=0;
   else
       dhabituation=spks2(:,t-1)-alpha hab*habituation(:,t-1);
       habituation(:,t)=habituation(:,t-1)+dhabituation;
       habituation(hab fire,t)=0;
   end
   hab fire=habituation(:,t)>=vth hab;
   habituation(hab fire,t)=vth hab;
   habituation(hab fire,t+1)=0;
habituation all(:,t)=[hab fire;hab fire;hab fire;hab fire;hab fire;hab fir
e];
   INN=Pre PWM norm(:,t)*10;
   INN T=transpose(INN);
   for i=1:1:6
       if t==1
           Input3 weighted(i,t)=INN T((i-1)*100+1:i*100)*w((i-
1) *100+1:i*100,1);
       else
           Input3 weighted(i,t)=INN T((i-1)*100+1:i*100)*w((i-
1) *100+1:i*100,t-1);
       end
   end
  Input3 weighted;
   %update vectorized ODE-----
   dv3=(15*Input3 weighted(:,t)-k n3tau*v3(:,t))*dt;
   %dv3 2=floor(dv3*100)/100;
   if t==1 || t==tint
       v3(:,t)=0;
   else
       inhib=sum(fired3);
       v3(:,t) = v3(:,t-1)+ 0.008*dv3-1.5*inhibit weak-inhibit strong-
0.05*inhib;%+0.5*Exc OUT(:,t)-Inh OUT(:,t);
   end
   0%_____
   %adding noise-----
   if t>2000 && t<7000
       %disp('noise');
       for i=1:6
          v3(i,t) = awgn(v3(i,t),20);
```

```
end
    end
    8----
    %handle spikes ( reset v )
    inhibit weak=zeros(6,1); %take points off only one time. and then let
it be.
    fired3 = v3(:,t)>= vth3(:,1); % neurons fired? find the ones whose
membrane potential is greater than vth
    %inhibit weak=inhibit weak+sum(fired3);
    inhibit weak(fired3)=10;
    v3(fired3, t) = 5;
    v3(fired3, t+1) = 0;
    % This part is added because there are multiple neurons firing
    %bc of the fact that we cannot have small steps of time. Smaller time
    %steps will cause speed degredation by a lot. So we'll let more
neurons
    %to fire and then do some compuation to get rid of the ones we dont
    %want.
    if t==1
        NumberFired(t) = 0;
    else
        NumberFired(t) = NumberFired(t-1) + sum(fired3);
    end
    if NumberFired(t)>3
        SORT ME=sort(v3(:,t-1),'descend');
        if SORT ME(1) == SORT ME(2)
            tt=find(v3(:,t-1)==SORT ME(1));
            MAX Indx(1)=tt(1);
            MAX Indx(2) =tt(2);
            for j=3:6
                MAX Indx(j)=find(v3(:,t-1)==SORT ME(j));
            end
        else
            for j=1:6
                MAX Indx(j)=find(v3(:,t-1)==SORT ME(j));
            end
        end
        if NumberFired(t) == 4
            for i=0:2:4
                if sum(fired3)-NumberFired(t-1)==i
                     fired3(MAX Indx(i/2+2))=0;
                     v3(MAX Indx(i/2+2),t)=0;
                end
                NumberFired(t) = 0;
            end
        elseif NumberFired(t) == 5
            for i=1:2:5
                if sum(fired3)-NumberFired(t-1)==i
```

```
fired3(MAX Indx(i/2+3/2:i/2+5/2))=0;
               v3(MAX Indx(i/2+3/2:i/2+5/2),t)=0;
           end
           NumberFired(t) = 0;
       end
   elseif NumberFired(t) == 6
       for i=2:2:6
          if sum(fired3)-NumberFired(t-1)==i
              fired3(MAX Indx(i/2+1:i/2+3))=0;
              v3(MAX Indx(i/2+1:i/2+3))=0;
          end
       end
       NumberFired(t) = 0;
   end
end
%CONTROL THE FIRING RATE -----
posts CTRL(:,t)=fired3;
if t==1
   FR_CTRL(:,t)=0.75;
else
   dFR1=posts CTRL(:,t-1)-kCTRL*FR CTRL(:,t-1);
   FR1(:,t) = FR1(:,t-1) + dFR1;
   FR CTRL(:,t)=0.75+FR1(:,t);
end
FR fire neg=FR CTRL(:,t)>=vth CTRL neg;
FR fire pos=FR CTRL(:,t)<=vth CTRL pos;</pre>
FR CTRL(FR fire neg,t)=vth CTRL neg;
FR CTRL(FR fire pos,t)=vth CTRL pos;
FR1(FR fire neg,t)=0;
FR1(FR fire pos,t)=0;
check fire(:,t)=FR fire pos;
§____
                                _____
          _____
%NEURAL STATE MACHINE------
Index=1;
dCombDtct=zeros(NumofOutput,1);
dCombDtct2=zeros(NumofOutput, 1);
dCombDtct1=zeros(NumofOutput,1);
%combinations of 1-----
combMAT1=nchoosek(1:NumofOutput,1);
for m=1:size(combMAT1,1)
   if t==1 || t==tint
       dCombDtct1(m) = 0;
   else
       dCombDtct1(m) = (sum(fired3(combMAT1(m,:))));
   end
```

```
106
```

```
if t==1 || t==tint
    CombDtct1(:,t)=0;
else
    CombDtct1(:,t)=CombDtct1(:,t-1)+dCombDtct1;
    CombDtct1(CombFired1,t)=0;
end
CombFired1=CombDtct1(:,t)==2;
CombDtct1(CombFired1,t)=2;
%combinations of 2-----
combMAT2=nchoosek(1:NumofOutput,2);
for m=1:size(combMAT2,1)
    if t==1 || t==tint
        dCombDtct2(m) = 0;
    else
        dCombDtct2(m) = (sum(fired3(combMAT2(m,:))));
    end
end
if t==1 || t==tint
   CombDtct2(:,t)=0;
else
    CombDtct2(:,t)=CombDtct2(:,t-1)+dCombDtct2;
    CombDtct2(CombFired2,t)=0;
end
CombFired2=CombDtct2(:,t)==2;
CombDtct2(CombFired2,t)=2;
%combinations of 3-----
combMAT=nchoosek(1:NumofOutput, NumofOutput/2);
for k=1:size(combMAT,1)
    if t==1 || t==tint
        dCombDtct(k)=0;
    else
        dCombDtct(k) = (sum(fired3(combMAT(k,:))));
    end
end
if t==1 || t==tint
    CombDtct(:,t)=0;
else
    CombDtct(:,t)=CombDtct(:,t-1)+dCombDtct;
    CombDtct(CombFired, t) = 0;
end
```

end

```
CombFired=CombDtct(:,t)>=vth comb;
CombDtct(CombFired,t)=vth comb;
```

```
inhibit neuron=sum(CombFired);
inhibit strong=(inhibit neuron>=1)*5;
```

```
spk comb=double(CombDtct(:,t)==vth comb);
   spk comb1=double(CombDtct1(:,t)==vth comb1);
   ∞_____
   % Homeostatis SINGLE------
   if t==1
       OUTPUT homeo1(:,t)=0.75;
       fired homeo pos1=1;
       fired homeo neg1=1;
       homeo_pos_spike1(:,t)=0;
       homeo neg spike1(:,t)=0;
   else
   dOUT1=(spk comb1-k homeo*OUTPUT homeo1(:,t-1))*dt;
   OUT1 homeo(:,t)=OUT1 homeo(:,t-1)+1*dOUT1;
   OUT1 homeo(fired homeo pos1,t)=0; %to reset the value after firing
   OUT1 homeo (fired homeo neg1,t)=0; %to reset the value after firing
   OUTPUT homeo1(:,t)=OUT1 homeo(:,t)+0.75;
   OUTPUT homeo1(:,1)=0.75;
   fired homeo pos1=OUTPUT homeo1(:,t)>=vth homeo pos1;
   fired_homeo_neg1=OUTPUT_homeo1(:,t) <=vth_homeo_neg1;</pre>
   OUTPUT homeo1(fired homeo pos1,t)=vth homeo pos1;
   OUTPUT homeol(fired homeo negl,t)=vth homeo negl;
   homeo pos spike1(:,t)=fired homeo pos1;
   homeo neg spike1(:,t)=fired homeo neg1;
   end
   if t==1
       Exc1 OUT(:,1)=0;
       Inh1 OUT(:,1)=0;
   else
       %Excitatory Input to the output neuron OR INSTEAD WE CHANGE THE
       %THRESHOLD
       dExcl OUT=(homeo neg spike1(:,t-1)-k3 ex single*Excl OUT(:,t-
1))*dt;
       Exc1 OUT(:,t)=Exc1 OUT(:,t-1)+dExc1 OUT;
       %Inhibitory Input to the output neuron OR INSTEAD WE CHANGE THE
       %THRESHOLD
       dInh OUT1=(homeo pos spike1(:,t-1)-k3 single*Inh1 OUT(:,t-1))*dt;
       Inh1 OUT(:,t)=Inh1 OUT(:,t-1)+dInh OUT1;
       if Exc1 OUT(:,t)<=0</pre>
           Exc1 OUT(:,t)=0;
       end
       if Inh1 OUT(:,t)<=0</pre>
           Inh1 OUT(:,t)=0;
       end
```

```
end
8---
    _____
%Homeostasis TRIPLE------
if t==1
    OUTPUT homeo3(:,t)=0.75;
    fired homeo pos3=1;
    fired homeo neg3=1;
    homeo pos spike(:,t)=0;
    homeo_neg_spike(:,t)=0;
else
Spike Comb time(:,t)=spk comb;
dOUT3=(spk comb-k homeo*OUTPUT homeo3(:,t-1))*dt;
OUT3 homeo(:,t)=OUT3 homeo(:,t-1)+1*dOUT3;
OUT3_homeo(fired_homeo_pos3,t)=0; %to reset the value after firing
OUT3_homeo(fired_homeo_neg3,t)=0; %to reset the value after firing
OUTPUT homeo3(:,t)=OUT3 homeo(:,t)+0.75;
OUTPUT homeo3(:,1)=0.75;
fired homeo pos3=OUTPUT homeo3(:,t)>=vth homeo pos3;
fired homeo neg3=OUTPUT homeo3(:,t)<=vth homeo neg3;</pre>
OUTPUT homeo3(fired homeo pos3,t)=vth homeo pos3;
OUTPUT homeo3(fired homeo neg3,t)=vth homeo neg3;
homeo pos spike(:,t)=fired homeo pos3;
homeo neg spike(:,t)=fired homeo neg3;
end
for i=1:NumofOutput
    FindIndx=find(combMAT==i);
    GR20=find(20<FindIndx & FindIndx<=40);</pre>
    GR40=find(FindIndx>40);
    FindIndx(GR20) = FindIndx(GR20) - 20;
    FindIndx(GR40) = FindIndx(GR40) - 40;
    spike inhib(i,t)=sum(homeo pos spike(FindIndx,t));
    spike exc(i,t)=sum(homeo neg spike(FindIndx,t));
end
if t==1
    Exc OUT(:,1)=0;
    Inh OUT(:,1)=0;
else
    %Excitatory Input to the output neuron OR INSTEAD WE CHANGE THE
    %THRESHOLD
    dExc OUT=(spike exc(:,t-1)-k3 ex*Exc OUT(:,t-1))*dt;
    Exc OUT(:,t)=Exc OUT(:,t-1)+dExc OUT;
```

%Inhibitory Input to the output neuron OR INSTEAD WE CHANGE THE

```
%THRESHOLD
```

```
dInh OUT=(spike inhib(:,t-1)-k3*Inh OUT(:,t-1))*dt;
       Inh OUT(:,t)=Inh OUT(:,t-1)+dInh OUT;
       if Exc OUT(:,t)<=0</pre>
          Exc OUT(:,t)=0;
       end
       if Inh OUT(:,t)<=0</pre>
           Inh OUT(:,t)=0;
       end
   end
   if t==1
       CTRL UP vth(:,t)=0;
       CTRL DN vth(:,t)=0;
   else
       CTRL UP vth(:,t)=CTRL UP vth(:,t-1)+FR fire neg;
       CTRL DN vth(:,t)=CTRL DN vth(:,t-1)+FR fire pos;
   end
   %vth3(:,1)=vth3 nominal+0.025*Inh OUT(:,t)-
0.011*Exc OUT(:,t)+0.025*Inh1 OUT(:,t)-0.011*Exc1 OUT(:,t);
   vth3(:,1)=vth3 nominal+0.025*Inh OUT(:,t)-
0.01*Exc OUT(:,t);%+0.011*Inh1 OUT(:,t)-0.011*Exc1 OUT(:,t);
   for i=1:7
       if t>2*(i*15400-1400) && t<2*(i*15400)
          vth3(:,1)=vth time(:,i*15400-1400);
       end
   end
   vth time(:,t)=vth3;
   %END OF HOMEOSTASIS-----
   % WEIGHT UPDATE-----
   %SR latch output
   %POSITIVE WEIGHT CHANGE-----
   %decay in time
   dLInt1=(Pre(:,t)-alpha*LInt1(:,t))*dt;
   LInt1(:,t+1)=LInt1(:,t)+dLInt1;
   % SR-leaky integrator (SR minus decay)
   y1 STDP(:,t)=Pre PWM(:,t)-LInt1(:,t);
   %y1 STDP(:,t)=LInt1(:,t);
   for j=1:6
```

```
posts((j-1)*100+1:j*100,t)=fired3(j);
   end
   dwP(:,t)=posts(:,t).*y1 STDP(:,t)*LRateP;
   Post PWM(:,t+1)=Post PWM(:,t)+posts(:,t);
   %NEGATIVE WEIGHT CHANGE-----
   %decay in time
   dOUT2=(posts(:,t)-alpha*LInt2(:,t))*dt;
   LInt2(:,t+1)=LInt2(:,t)+dOUT2;
   y2 STDP(:,t)=Post PWM(:,t)-alpha*LInt2(:,t);
   % SR-decay
dwN(:,t)=Pre(:,t).*y2 STDP(:,t)*LRateN+~Pre PWM(:,t).*posts(:,t)*LRateN;
   dw(:,t) = 0.3*(dwP(:,t) - dwN(:,t)) - 0.0081*exp(-
0.00003*t) * habituation all(:,t);
   if t==1
       w(:, t) = IC;
   else
       w(:,t) = w(:,t-1) + dw(:,t);
   end
   for i=1:n 2ndLayer*n 3rdLayer
       if w(i,t) >= 0.7
          w(i,t) = 0.7;
       elseif w(i,t) <=-0.01</pre>
          w(i,t) = -0.01;
       end
   end
8-----
              _____
end
%Plot Pre spikes
%figure(1)
%plot (X 2(idx 2),Y3 2(idx 2),['r','.']);
%xlim([0,T*dt]);
%ylim([0,n 2ndLayer]);
%Plot spike raster
figure(2)
spks3 = double(v3==5);
clf , hold on ;
[X 3,Y3 3] = meshgrid((0:T-1)*dt,1:n 3rdLayer) ;
idx 3 = find(spks3==1);
plot (X 3(idx 3),Y3 3(idx 3) ,['r','.'] );
xlim([0,T*dt]);
ylim([0,n 3rdLayer]);
xlabel('Time[ms]')
ylabel('Unit #')
%plot weights-----
%for i=1:6
% figure(i+2)
 % plot((0:T-1)*dt,w((i-1)*100+1:i*100,:));
```

%end